

# Solutions Manual for Physics for Scientists and Engineers with Modern Physics 5th Giancoli

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## CHAPTER 2: Describing Motion: Kinematics in One Dimension

### Responses to Questions

1. A car speedometer measures only speed. It does not give any information about the direction of motion, and so does not measure velocity.
2. If the velocity of an object is constant, the speed must also be constant. (A constant velocity means that the speed and direction are both constant.) If the speed of an object is constant, the velocity CAN vary. For example, a car traveling around a curve at constant speed has a varying velocity, since the direction of the velocity vector is changing.
3. If the velocity of an object is constant, the speed and the direction of travel must also be constant. If that is the case, then the average velocity is the same as the instantaneous velocity, because nothing about its velocity is changing. The ratio of displacement to elapsed time will not be changing, no matter the actual displacement or time interval used for the measurement.
4. There is no general relationship between the magnitude of speed and the magnitude of acceleration. For example, one object may have a large but constant speed. The acceleration of that object is then 0. Another object may have a small speed but be gaining speed, and therefore have a positive acceleration. So in this case the object with the greater speed has the lesser acceleration.  
  
Or consider two objects that are dropped from rest at different times. If we ignore air resistance, then the object dropped first will always have a greater speed than the object dropped second, but both will have the same acceleration of  $9.80 \text{ m/s}^2$ .
5. The accelerations of the motorcycle and the bicycle are the same, assuming that both objects travel in a straight line. Acceleration is the change in velocity divided by the change in time. The magnitude of the change in velocity in each case is the same, 10 km/h, so over the same time interval the accelerations will be equal.
6. Yes, for example, a car that is traveling northward and slowing down has a northward velocity and a southward acceleration.
7. The velocity of an object can be negative when its acceleration is positive. If we define the positive direction to be to the right, then an object traveling to the left that is slowing down will have a negative velocity with a positive acceleration.  
  
The velocity of an object can also be positive when its acceleration is negative. If again we define the positive direction to be to the right, then an object traveling to the right that is slowing down will have a positive velocity and a negative acceleration.
8. If north is defined as the positive direction, then an object traveling to the south and increasing in speed has both a negative velocity and a negative acceleration. Or, if "up" is defined as the positive direction, then an object falling due to gravity has both a negative velocity and a negative acceleration (if air resistance is ignored).
9. If the two cars emerge side by side, then the one moving faster is passing the other one. Thus car A is passing car B. With the acceleration data given for the problem, the ensuing motion would be that car A would pull away from car B for a time, but eventually car B would catch up to and pass car A.

10. Yes. Remember that acceleration is a *change in velocity* per unit time, or a *rate of change* in velocity. So, velocity can be increasing while the rate of increase goes down. For example, suppose a car is traveling at 40 km/h and one second later is going 50 km/h. One second after that, the car's speed is 55 km/h. The car's speed was increasing the entire time, but its acceleration in the second time interval was lower than in the first time interval. Thus its acceleration was decreasing even as the speed was increasing.

Another example would be an object falling WITH air resistance, but with a speed less than its terminal velocity. Let the downward direction be positive. As the object falls, it gains speed, and the air resistance increases. As the air resistance increases, the acceleration of the falling object decreases, and so it gains speed less quickly the longer it falls.

11. If there were no air resistance, the ball's only acceleration during flight would be the acceleration due to gravity, so the ball would land in the catcher's mitt with the same speed it had when it left the bat, 120 km/h. Since the acceleration is the same through the entire flight, the time for the ball's speed to change from 120 km/h to 0 on the way up is the same as the time for its speed to change from 0 to 120 km/h on the way down. In both cases the ball has the same magnitude of displacement.
12. (a) If air resistance is negligible, the acceleration of a freely falling object stays the same as the object falls. The object's speed increases, but since it increases at a constant rate, the acceleration is constant.  
(b) In the presence of air resistance, the acceleration decreases. Air resistance increases as the speed increases. If the object falls far enough, the acceleration will become zero and the velocity will become constant. That velocity is often called the terminal velocity.
13. Average speed is the displacement divided by the time. Since the distances from A to B and from B to C are equal, you spend more time traveling at 70 km/h than at 90 km/h, so your average speed should be less than 80 km/h. If the distance from A to B (or B to C) is  $x$  km, then the total distance traveled is  $2x$ . The total time required to travel this distance is  $x/70$  h plus  $x/90$  h. Then
- $$\bar{v} = \frac{d}{t} = \frac{2x}{x/70 + x/90} = \frac{2(90)(70)}{90 + 70} = 78.75 \text{ km/h} \approx 79 \text{ km/h}.$$
14. Yes. Consider an object thrown straight up in the air. It has a nonzero acceleration due to gravity for its entire flight (neglecting air resistance). However, at the highest point it momentarily has a zero velocity. A car, at the moment it starts moving from rest, has zero velocity and nonzero acceleration.
15. Yes. Any time the velocity is constant, the acceleration is zero. For example, a car traveling at a constant 90 km/h in a straight line has nonzero velocity and zero acceleration.
16. A rock falling from a cliff has a constant acceleration if air resistance is neglected. An elevator moving from the second floor to the fifth floor making stops along the way does NOT have a constant acceleration. Its acceleration will change in magnitude and direction as the elevator starts and stops. The dish resting on a table has a constant (zero) acceleration.
17. The two conditions are that the motion needs to be near the surface of the Earth, and that there is no air resistance. An example where the second condition is not even a reasonable approximation is that of parachuting. The air resistance caused by the parachute results in the acceleration not being constant, and having values much different than  $9.8 \text{ m/s}^2$ .

18. The slope of the position versus time curve is the velocity. The object starts at the origin with a constant velocity (and therefore zero acceleration), which it maintains for about 20 s. For the next 10 s, the positive curvature of the graph indicates the object has a positive acceleration; its speed is increasing. From 30 s to 45 s, the graph has a negative curvature; the object uniformly slows to a stop, changes direction, and then moves backwards with increasing speed. During this time interval its acceleration is negative, since the object is slowing down while traveling in the positive direction and then speeding up while traveling in the negative direction. For the final 5 s shown, the object continues moving in the negative direction but slows down, which gives it a positive acceleration. During the 50 s shown, the object travels from the origin to a point 20 m away, and then back 10 m to end up 10 m from the starting position.
19. Initially, the object begins with a speed of 14 m/s, moving in the positive direction with a constant acceleration, until  $t = 45$  s, when it has a velocity of about 37 m/s in the positive direction. The acceleration then decreases, reaching an instantaneous acceleration of 0 at  $t = 50$  s, when the object has its maximum speed of about 38 m/s. The object then begins to slow down, but continues to move in the positive direction. The object stops moving at  $t = 90$  s and stays at rest until  $t = 108$  s. Then the object begins to move in the positive direction again, at first with a larger acceleration, and then a lesser acceleration. At the end of the recorded motion, the object is still moving to the right and gaining speed.

## Responses to MisConceptual Questions

1. (d) It is a common misconception that a positive acceleration always increases the speed, as in (b) and (c). However, when the velocity and acceleration are in opposite directions the speed will decrease. TBEXAM.COM
2. (d) Since the velocity and acceleration are in opposite directions, the object will slow to a stop. However, since the acceleration remains constant, the object will only momentarily stop before moving toward the left.
3. (c) Since the distances are the same, a common error is to assume that the average speed will be halfway between the two speeds, or 40 km/h. However, it takes the car longer to travel the 4 km at 30 km/h than to travel the other 4 km at 50 km/h. Since more time is spent at 30 km/h the average speed will be closer to 30 km/h than to 50 km/h.
4. (d) From Eq. 2-12(c), for an object with constant acceleration starting from rest, the final speed is given by  $v = \sqrt{2ad}$ . Thus if  $a_B = 4a_A$ , then  $v_B = 2v_A$ .
5. (a) A common misconception is that the acceleration of an object in free-fall depends upon the motion of the object. If there is no air resistance, the acceleration is the same throughout the flight, even at the top. If the acceleration were 0 at the top, the object would not move since it also has a velocity of 0 at the top. The velocity is constantly changing throughout the flight.
6. (c) A common misconception is that the acceleration of an object in free-fall depends upon the motion of the object. If there is no air resistance, the accelerations for the two balls are the same magnitude and direction throughout both of their flights.
7. (a) Since the distance between the rocks increases with time, a common misconception is that the velocities are increasing at different rates. However, both rocks fall under the influence of gravity, so their velocities increase at the same rate.

8. (e) Both objects experience the same acceleration, so the rock that is dropped first always has a higher speed than the second rock. Since the first rock is always moving faster, it is always getting farther away from the second rock.
9. (b, c) Each of the given equations are based on Eq. 2-12(a-d). Answer (a) has the acceleration replaced properly with  $-g$ , but the initial velocity is downward and as such should be negative. Answer (d) is incorrect because the initial velocity has been inserted for the average velocity. Answers (b) and (c) have the correct signs for each variable and the known values are inserted properly.
10. (a) Increasing speed means that the slope must be getting steeper over time. In graphs (b) and (e) the slope remains constant, so these are cars moving at constant speed. In graph (c), as time increases  $x$  decreases. However the rate at which it decreases is also decreasing. This is a car slowing down. In graph (d) the car is moving away from the origin, but again it is slowing down. The only graph in which the slope is increasing with time is graph (a).
11. (c, e) The two lines have different slopes at point  $A$ , so they don't have the same instantaneous velocity or speed. The object represented by the dashed line has traveled more distance, since it has traveled "forward and back" to get to the point represented by  $A$ . But they are both at the same position after the same amount of time, and so they have the same average velocity.

## Solutions to Problems

1. The distance of travel (displacement) can be found by rearranging Eq. 2-2 for the average velocity. Also note that the units of the velocity and the time are not the same, so the speed units will be converted.

$$\bar{v} = \Delta x / \Delta t \rightarrow \Delta x = \bar{v} \Delta t = (85 \text{ km/h}) \left( \frac{1 \text{ h}}{3600 \text{ s}} \right) (2.0 \text{ s}) = 0.0472 \text{ km} \approx \boxed{47 \text{ m}}$$

2. The average speed is given by Eq. 2-1, using  $d$  to represent distance traveled.

$$\bar{v} = d / \Delta t = 235 \text{ km} / 2.85 \text{ h} = \boxed{82.5 \text{ km/h}}$$

3. The average velocity is given by Eq. 2-2.

$$\bar{v} = \frac{\Delta x}{\Delta t} = \frac{8.5 \text{ cm} - 5.2 \text{ cm}}{3.4 \text{ s} - (-2.0 \text{ s})} = \frac{3.3 \text{ cm}}{5.4 \text{ s}} = \boxed{0.61 \text{ cm/s}}$$

The average speed cannot be calculated. To calculate the average speed, we would need to know the actual distance traveled, and it is not given. We only have the displacement.

4. (a) The speed of sound is intimated in the problem as 1 mile per 5 seconds. The speed is calculated as follows.

$$\text{speed} = \frac{\text{distance}}{\text{time}} = \left( \frac{1 \text{ mi}}{5 \text{ s}} \right) \left( \frac{1610 \text{ m}}{1 \text{ mi}} \right) = 322 \text{ m/s} \approx \boxed{300 \text{ m/s}}$$

- (b) The speed of 322 m/s would imply the sound traveling a distance of 966 meters (which is approximately 1 km) in 3 seconds. So the rule could be approximated as 1 km every 3 s.

5. The time for the first part of the trip is calculated from the initial speed and the first distance, using  $d$  to represent distance.

$$\bar{v}_1 = \frac{d_1}{\Delta t_1} \rightarrow \Delta t_1 = \frac{d_1}{\bar{v}_1} = \frac{210 \text{ km}}{95 \text{ km/h}} = 2.211 \text{ h}$$

The time for the second part of the trip is now calculated.

$$\Delta t_2 = \Delta t_{\text{total}} - \Delta t_1 = 4.5 \text{ h} - 2.211 \text{ h} = 2.289 \text{ h}$$

The distance for the second part of the trip is calculated from the average speed for that part of the trip and the time for that part of the trip.

$$\bar{v}_2 = \frac{d_2}{\Delta t_2} \rightarrow d_2 = \bar{v}_2 \Delta t_2 = (65 \text{ km/h})(2.289 \text{ h}) = 148.8 \text{ km} \approx 150 \text{ km}$$

(a) The total distance is then  $d_{\text{total}} = d_1 + d_2 = 210 \text{ km} + 148.8 \text{ km} = 358.8 \text{ km} \approx \boxed{360 \text{ km}}$ .

(b) The average speed is NOT the average of the two speeds, and so is NOT 85 km/h. Use the definition of average speed, Eq. 2-1.

$$\bar{v} = \frac{d_{\text{total}}}{\Delta t_{\text{total}}} = \frac{358.8 \text{ km}}{4.5 \text{ h}} = 79.73 \text{ km/h} \approx \boxed{80 \text{ km/h}}$$

Note that the result has 2 significant figures, and so could be expressed as  $8.0 \times 10^1 \text{ km/h}$ .

6. The distance traveled is  $38 \text{ m} + \frac{1}{2}(38 \text{ m}) = 57 \text{ m}$ , and the displacement is  $38 \text{ m} - \frac{1}{2}(38 \text{ m}) = 19 \text{ m}$ . The total time is  $7.4 \text{ s} + 1.8 \text{ s} = 9.2 \text{ s}$ .

(a) Average speed =  $\frac{\text{distance}}{\text{time elapsed}} = \frac{57 \text{ m}}{9.2 \text{ s}} = \boxed{6.2 \text{ m/s}}$

(b) Average velocity =  $v_{\text{avg}} = \frac{\text{displacement}}{\text{time elapsed}} = \frac{19 \text{ m}}{9.2 \text{ s}} = \boxed{2.1 \text{ m/s}}$

7. The distance traveled is 3200 m ( $8 \text{ laps} \times 400 \text{ m/lap}$ ). That distance probably has either 3 or 4 significant figures, since the track distance is probably known to at least the nearest meter for competition purposes. The displacement is 0 because the ending point is the same as the starting point.

(a) Average speed =  $\frac{d}{\Delta t} = \frac{3200 \text{ m}}{14.5 \text{ min}} \left( \frac{1 \text{ min}}{60 \text{ s}} \right) = \boxed{3.68 \text{ m/s}}$

(b) Average velocity =  $\bar{v} = \Delta x / \Delta t = \boxed{0 \text{ m/s}}$

8. The average speed is the distance divided by the time.

$$\bar{v} = \frac{d}{t} = \left( \frac{1 \times 10^9 \text{ km}}{1 \text{ yr}} \right) \left( \frac{1 \text{ yr}}{365.25 \text{ d}} \right) \left( \frac{1 \text{ d}}{24 \text{ h}} \right) = 1.141 \times 10^5 \text{ km/h} \approx \boxed{1 \times 10^5 \text{ km/h}}$$

9. Both objects will have the same time of travel. If the truck travels a distance  $\Delta x_{\text{truck}}$ , then the distance the car travels will be  $\Delta x_{\text{car}} = \Delta x_{\text{truck}} + 310 \text{ m}$ . Use Eq. 2-2 for average speed,  $\bar{v} = \Delta x / \Delta t$ , solve for time, and equate the two times.

$$\Delta t = \frac{\Delta x_{\text{truck}}}{\bar{v}_{\text{truck}}} = \frac{\Delta x_{\text{car}}}{\bar{v}_{\text{car}}} \quad \frac{\Delta x_{\text{truck}}}{75 \text{ km/h}} = \frac{\Delta x_{\text{truck}} + 310 \text{ m}}{95 \text{ km/h}}$$

Solving for  $\Delta x_{\text{truck}}$  gives  $\Delta x_{\text{truck}} = (310 \text{ m}) \frac{(75 \text{ km/h})}{(95 \text{ km/h} - 75 \text{ km/h})} = 1163 \text{ m}$ .

The time of travel is  $\Delta t = \frac{\Delta x_{\text{truck}}}{\bar{v}_{\text{truck}}} = \left( \frac{1163 \text{ m}}{75000 \text{ m/h}} \right) \left( \frac{60 \text{ min}}{1 \text{ h}} \right) = 0.9304 \text{ min} = 55.82 \text{ s} \approx \boxed{56 \text{ s}}$ .

Also note that  $\Delta t = \frac{\Delta x_{\text{car}}}{\bar{v}_{\text{car}}} = \left( \frac{1163 \text{ m} + 310 \text{ m}}{95000 \text{ m/h}} \right) \left( \frac{60 \text{ min}}{1 \text{ h}} \right) = 0.9303 \text{ min} = 56 \text{ s}$ .

#### ALTERNATE SOLUTION:

The speed of the car relative to the truck is  $95 \text{ km/h} - 75 \text{ km/h} = 20 \text{ km/h}$ . In the reference frame of the truck, the car must travel 310 m to catch it.

$$\Delta t = \frac{0.31 \text{ km}}{20 \text{ km/h}} \left( \frac{3600 \text{ s}}{1 \text{ h}} \right) = 56 \text{ s}$$

10. The distance traveled is 560 km (280 km outgoing, 280 km return). The displacement ( $\Delta x$ ) is 0 because the ending point is the same as the starting point.

(a) To find the average speed, we need the distance traveled (560 km) and the total time elapsed. During the outgoing portion,  $\bar{v}_1 = \frac{\Delta x_1}{\Delta t_1}$  and so  $\Delta t_1 = \frac{\Delta x_1}{\bar{v}_1} = \frac{280 \text{ km}}{95 \text{ km/h}} = 2.947 \text{ h}$ .

During the return portion,  $\bar{v}_2 = \frac{\Delta x_2}{\Delta t_2}$ , and so  $\Delta t_2 = \frac{\Delta x_2}{\bar{v}_2} = \frac{280 \text{ km}}{55 \text{ km/h}} = 5.091 \text{ h}$ . Thus the

total time, including lunch, is  $\Delta t_{\text{total}} = \Delta t_1 + \Delta t_{\text{lunch}} + \Delta t_2 = 2.947 \text{ h} + 1 \text{ h} + 5.091 \text{ h} = 9.038 \text{ h}$ .

$$\bar{v} = \frac{\Delta x_{\text{total}}}{\Delta t_{\text{total}}} = \frac{560 \text{ km}}{9.038 \text{ h}} = 61.96 \text{ km/h} \approx \boxed{62 \text{ km/h}}$$

(b) To find the average velocity, use the displacement and the elapsed time. The displacement is 0 since the person returns to their starting point.

$$\boxed{\bar{v} = \Delta x / \Delta t = 0}$$

11. Since the locomotives have the same speed, they each travel half the distance, 4.75 km. Find the time of travel from the average speed.

$$\bar{v} = \frac{\Delta x}{\Delta t} \rightarrow \Delta t = \frac{\Delta x}{\bar{v}} = \frac{4.75 \text{ km}}{155 \text{ km/h}} = 0.03065 \text{ h} \left( \frac{60 \text{ min}}{1 \text{ h}} \right) = 1.839 \text{ min} \approx \boxed{1.8 \text{ min}}$$

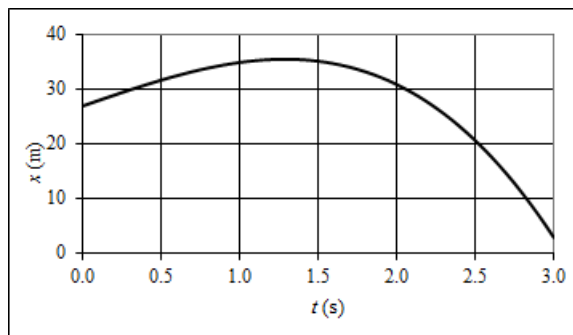
12. (a) The area between the concentric circles is equal to the length times the width of the spiral path.

$$\pi R_2^2 - \pi R_1^2 = w\ell \rightarrow$$

$$\ell = \frac{\pi(R_2^2 - R_1^2)}{w} = \frac{\pi[(0.058 \text{ m})^2 - (0.025 \text{ m})^2]}{1.6 \times 10^{-6} \text{ m}} = 5.378 \times 10^3 \text{ m} \approx \boxed{5400 \text{ m}}$$

$$(b) \quad 5.378 \times 10^3 \text{ m} \left( \frac{1 \text{ s}}{1.2 \text{ m}} \right) \left( \frac{1 \text{ min}}{60 \text{ s}} \right) = 74.69 \text{ min} \approx \boxed{75 \text{ min}}$$

13. (a)



(b) The average velocity is the displacement divided by the elapsed time.

$$\bar{v} = \frac{x(3.0) - x(0.0)}{3.0\text{ s} - 0.0\text{ s}} = \frac{[27 + 10(3.0) - 2(3.0)^3]\text{ m} - (27\text{ m})}{3.0\text{ s}} = \boxed{-8.0\text{ m/s}}$$

(c) The instantaneous velocity is given by the derivative of the position function.

$$v = \frac{dx}{dt} = (10 - 6t^2)\text{ m/s} \quad 10 - 6t^2 = 0 \rightarrow t = \sqrt{\frac{5}{3}}\text{ s} = \boxed{1.3\text{ s}}$$

This can be seen from the graph as the “highest” point on the graph.

14. The average speed for each segment of the trip is given by  $\bar{v} = \frac{d}{\Delta t}$ , so  $\Delta t = \frac{d}{\bar{v}}$  for each segment.

$$\text{For the first segment, } \Delta t_1 = \frac{d_1}{\bar{v}_1} = \frac{1900\text{ km}}{720\text{ km/h}} = 2.639\text{ h.}$$

$$\text{For the second segment, } \Delta t_2 = \frac{d_2}{\bar{v}_2} = \frac{2700\text{ km}}{990\text{ km/h}} = 2.727\text{ h.}$$

$$\text{Thus the total time is } \Delta t_{\text{tot}} = \Delta t_1 + \Delta t_2 = 2.639\text{ h} + 2.727\text{ h} = 5.366\text{ h} \approx \boxed{5.4\text{ h}}.$$

The average speed of the plane for the entire trip is

$$\bar{v} = \frac{d_{\text{tot}}}{\Delta t_{\text{tot}}} = \frac{1900\text{ km} + 2700\text{ km}}{5.366\text{ h}} = 857.2\text{ km/h} \approx \boxed{860\text{ km/h}}.$$

Note that Eq. 2–12d does NOT apply in this situation. The numeric average of the two speeds is 855 km/h.

15. In order for the two ships to meet “in the middle,” they must both have the same average velocity (ignoring their different directions). We can find the time for each segment of the trip using

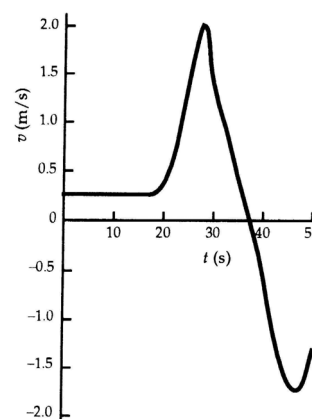
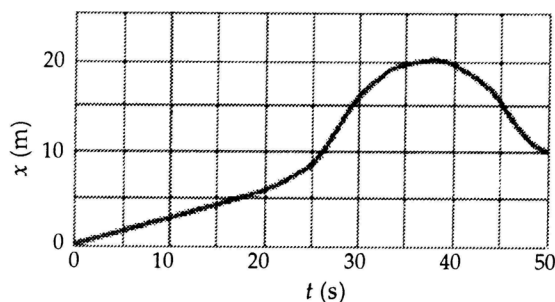
$$\bar{v} = \frac{d}{\Delta t}, \text{ so } \Delta t = \frac{d}{\bar{v}} \text{ for each segment. Both ships travel } 600\text{ km} + 800\text{ km} + 600\text{ km} = 2000\text{ km.}$$

$$\text{First ship: } \Delta t = \frac{d_1}{\bar{v}_1} + \frac{d_2}{\bar{v}_2} + \frac{d_3}{\bar{v}_3} = \frac{600\text{ km}}{20\text{ km/h}} + \frac{800\text{ km}}{40\text{ km/h}} + \frac{600\text{ km}}{20\text{ km/h}} = 80\text{ h}$$

$$\text{Second ship: } \bar{v} = \frac{d}{\Delta t} = \frac{2000\text{ km}}{80\text{ h}} = \boxed{25\text{ km/h}}$$

16. Slightly different answers may be obtained since the data comes from reading the graph.
- (a) The instantaneous velocity is given by the slope of the tangent line to the curve. At  $t = 10.0\text{ s}$ , the slope is approximately  $v(10) \approx \frac{3\text{ m} - 0}{10.0\text{ s} - 0} = \boxed{0.3\text{ m/s}}$ .
- (b) At  $t = 30.0\text{ s}$ , the slope of the tangent line to the curve, and thus the instantaneous velocity, is approximately  $v(30) \approx \frac{20\text{ m} - 8\text{ m}}{35\text{ s} - 25\text{ s}} = \boxed{1.2\text{ m/s}}$ .
- (c) The average velocity is given by  $\bar{v} = \frac{x(5.0) - x(0)}{5.0\text{ s} - 0\text{ s}} = \frac{1.5\text{ m} - 0}{5.0\text{ s}} = \boxed{0.30\text{ m/s}}$ .
- (d) The average velocity is given by  $\bar{v} = \frac{x(30.0) - x(25.0)}{30.0\text{ s} - 25.0\text{ s}} = \frac{16\text{ m} - 9\text{ m}}{5.0\text{ s}} = \boxed{1.4\text{ m/s}}$ .
- (e) The average velocity is given by  $\bar{v} = \frac{x(50.0) - x(40.0)}{50.0\text{ s} - 40.0\text{ s}} = \frac{10\text{ m} - 19.5\text{ m}}{10.0\text{ s}} = \boxed{-0.95\text{ m/s}}$ .
17. Slightly different answers may be obtained since the data comes from reading the graph.
- (a) The indication of a constant velocity on a position-time graph is a constant slope, which occurs from  $t = 0\text{ s}$  to  $t \approx 18\text{ s}$ .
- (b) The greatest velocity will occur when the slope is the highest positive value, which occurs at  $t \approx 27\text{ s}$ .
- (c) The indication of a 0 velocity on a position-time graph is a slope of 0, which occurs at  $t \approx 38\text{ s}$ .
- (d) TBEXAM.COM The object moves in both directions. When the slope is positive, from  $t = 0\text{ s}$  to  $t \approx 38\text{ s}$ , the object is moving in the positive direction. When the slope is negative, from  $t \approx 38\text{ s}$  to  $t = 50\text{ s}$ , the object is moving in the negative direction.

18. The  $v$  vs.  $t$  graph is found by taking the slope of the  $x$  vs.  $t$  graph. Both graphs are shown here.



19. The average speed of sound is given by  $v_{\text{sound}} = \Delta x / \Delta t$ , and so the time for the sound to travel from the end of the lane back to the bowler is  $\Delta t_{\text{sound}} = \frac{\Delta x}{v_{\text{sound}}} = \frac{16.5\text{ m}}{340\text{ m/s}} = 4.85 \times 10^{-2}\text{ s}$ . Thus the time for the ball to travel from the bowler to the end of the lane is given by  $\Delta t_{\text{ball}} = \Delta t_{\text{total}} - \Delta t_{\text{sound}} =$

$2.75\text{ s} - 4.85 \times 10^{-2}\text{ s} = 2.7015\text{ s}$ . And so the speed of the ball is as follows.

$$v_{\text{ball}} = \frac{\Delta x}{\Delta t_{\text{ball}}} = \frac{16.5\text{ m}}{2.7015\text{ s}} = 6.1077\text{ m/s} \approx \boxed{6.11\text{ m/s}}$$

20. For the car to pass the train, the car must travel the length of the train AND the distance the train travels. The distance the car travels can thus be written as either  $d_{\text{car}} = v_{\text{car}}t = (95\text{ km/h})t$  or  $d_{\text{car}} = \ell_{\text{train}} + v_{\text{train}}t = 1.50\text{ km} + (75\text{ km/h})t$ . To solve for the time, equate these two expressions for the distance the car travels.

$$(95\text{ km/h})t = 1.50\text{ km} + (75\text{ km/h})t \rightarrow t = \frac{1.50\text{ km}}{20\text{ km/h}} = 0.075\text{ h} \left( \frac{60\text{ min}}{1\text{ h}} \right) = \boxed{4.5\text{ min}}$$

Note that this is the same as calculating from the reference frame of the train, in which the car is moving at 20 km/h and must travel the length of the train.

The distance the car travels during this time is  $d = (95\text{ km/h})(0.075\text{ h}) = 7.125\text{ km} \approx \boxed{7.1\text{ km}}$ .

If the train is traveling in the opposite direction from the car, then the car must travel the length of the train MINUS the distance the train travels. Thus the distance the car travels can be written as either  $d_{\text{car}} = (95\text{ km/h})t$  or  $d_{\text{car}} = 1.50\text{ km} - (75\text{ km/h})t$ . To solve for the time, equate these two expressions for the distance the car travels.

$$(95\text{ km/h})t = 1.50\text{ km} - (75\text{ km/h})t \rightarrow$$

$$t = \frac{1.50\text{ km}}{170\text{ km/h}} = 8.824 \times 10^{-3}\text{ h} \left( \frac{3600\text{ s}}{1\text{ h}} \right) = 31.8\text{ s} \approx \boxed{32\text{ s}}$$

The distance the car travels during this time is  $d = (95\text{ km/h})(8.824 \times 10^{-3}\text{ h}) = \boxed{0.84\text{ km}}$ .

21. (a) The average acceleration of the sprinter is  $\bar{a} = \frac{\Delta v}{\Delta t} = \frac{9.00\text{ m/s} - 0.00\text{ m/s}}{1.48\text{ s}} = \boxed{6.08\text{ m/s}^2}$ .  
 (b) We change the units for the acceleration.

$$\bar{a} = (6.08\text{ m/s}^2) \left( \frac{1\text{ km}}{1000\text{ m}} \right) \left( \frac{3600\text{ s}}{1\text{ h}} \right)^2 = \boxed{7.88 \times 10^4\text{ km/h}^2}$$

22. The initial velocity is  $v_0 = 15\text{ km/h}$ , the final velocity is  $v = 65\text{ km/h}$ , and the displacement is  $x - x_0 = 4.0\text{ km} = 4000\text{ m}$ . Find the average acceleration from Eq. 2-12c.

$$v^2 = v_0^2 + 2a(x - x_0) \rightarrow$$

$$a = \frac{v^2 - v_0^2}{2(x - x_0)} = \frac{[(65\text{ km/h})^2 - (15\text{ km/h})^2] \left( \frac{1\text{ m/s}}{3.6\text{ km/h}} \right)^2}{2(4000\text{ m})} = \boxed{3.9 \times 10^{-2}\text{ m/s}^2}$$

23. The initial velocity of the car is the average velocity of the car before it accelerates.

$$\bar{v} = \frac{\Delta x}{\Delta t} = \frac{120\text{ m}}{5.0\text{ s}} = 24\text{ m/s} = v_0$$

The final velocity is  $v = 0$ , and the time to stop is 3.7 s. Use Eq. 2-12a to find the acceleration.

$$v = v_0 + at \rightarrow a = \frac{v - v_0}{t} = \frac{0 - 24 \text{ m/s}}{3.7 \text{ s}} = -6.486 \text{ m/s}^2$$

Thus the magnitude of the acceleration is  $\boxed{6.5 \text{ m/s}^2}$ , or  $(6.486 \text{ m/s}^2) \left( \frac{1 \text{ g}}{9.80 \text{ m/s}^2} \right) = \boxed{0.66 \text{ g's}}$ .

24. We assume that the speedometer can read to the nearest km/h, and so the value of 120 km/h has three significant digits. The time can be found from the average acceleration,  $\bar{a} = \Delta v / \Delta t$ .

$$\Delta t = \frac{\Delta v}{\bar{a}} = \frac{120 \text{ km/h} - 65 \text{ km/h}}{1.8 \text{ m/s}^2} = \frac{(55 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right)}{1.8 \text{ m/s}^2} = 8.488 \text{ s} \approx \boxed{8.5 \text{ s}}$$

25. (a) The average velocity is the displacement divided by the elapsed time.

$$\bar{v} = \frac{\Delta x}{\Delta t} = \frac{385 \text{ m} - 25 \text{ m}}{20.0 \text{ s} - 3.00 \text{ s}} = \boxed{21.2 \text{ m/s}}$$

$$(b) \quad \bar{a} = \frac{\Delta v}{\Delta t} = \frac{45.0 \text{ m/s} - 11.0 \text{ m/s}}{20.0 \text{ s} - 3.00 \text{ s}} = \boxed{2.00 \text{ m/s}^2}$$

26. The acceleration is the second derivative of the position function.

$$x = 4.8t + 7.3t^2 \rightarrow v = \frac{dx}{dt} = 4.8 + 14.6t \rightarrow a = \frac{d^2x}{dt^2} = \frac{dv}{dt} = \boxed{14.6 \text{ m/s}^2}$$

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27. (a) Since the units of  $A$  times the units of  $t$  must equal meters, the units of  $A$  must be  $\boxed{\text{m/s}}$ .

Since the units of  $B$  times the units of  $t^2$  must equal meters, the units of  $B$  must be  $\boxed{\text{m/s}^2}$ .

- (b) The acceleration is the second derivative of the position function.

$$x = At + Bt^2 \rightarrow v = \frac{dx}{dt} = A + 2Bt \rightarrow a = \frac{d^2x}{dt^2} = \frac{dv}{dt} = \boxed{2B \text{ m/s}^2}$$

$$(c) \quad v = A + 2Bt \rightarrow v(5) = \boxed{(A + 12B) \text{ m/s}} \quad a = \boxed{2B \text{ m/s}^2}$$

- (d) The velocity is the derivative of the position function.

$$x = At + Bt^{-3} \rightarrow v = \frac{dx}{dt} = \boxed{A - 3Bt^{-4}}$$

28. To estimate the velocity, find the average velocity over each time interval, and assume that the car had that velocity at the midpoint of the time interval. To estimate the acceleration, find the average acceleration over each time interval, and assume that the car had that acceleration at the midpoint of the time interval. A sample of each calculation is shown.

From 2.00 s to 2.50 s, for average velocity:

$$t_{\text{mid}} = \frac{2.50 \text{ s} + 2.00 \text{ s}}{2} = 2.25 \text{ s}$$

$$v_{\text{avg}} = \frac{\Delta x}{\Delta t} = \frac{13.79 \text{ m} - 8.55 \text{ m}}{2.50 \text{ s} - 2.00 \text{ s}} = \frac{5.24 \text{ m}}{0.50 \text{ s}} = 10.48 \text{ m/s}$$

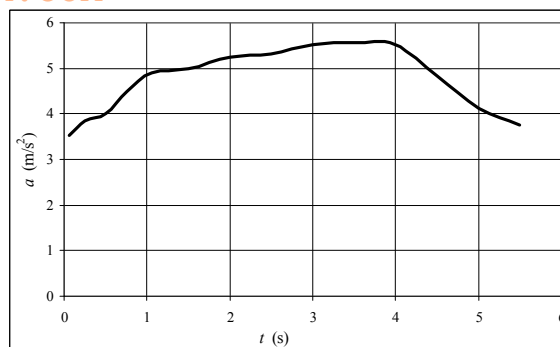
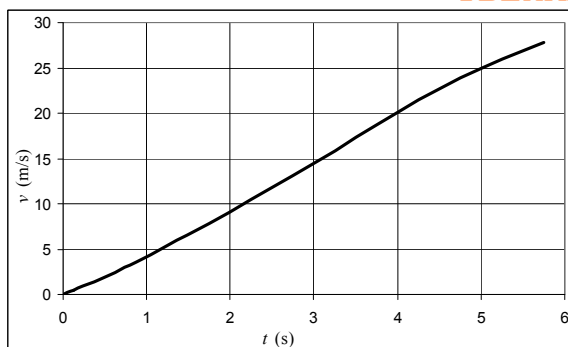
From 2.25 s to 2.75 s, for average acceleration:

$$t_{\text{mid}} = \frac{2.25 \text{ s} + 2.75 \text{ s}}{2} = 2.50 \text{ s}$$

$$a_{\text{avg}} = \frac{\Delta v}{\Delta t} = \frac{13.14 \text{ m/s} - 10.48 \text{ m/s}}{2.75 \text{ s} - 2.25 \text{ s}} = \frac{2.66 \text{ m/s}}{0.50 \text{ s}} = 5.32 \text{ m/s}^2$$

Table of Calculations

| $t$ (s) | $x$ (m) | $t$ (s) | $v$ (m/s) | $t$ (s) | $a$ (m/s <sup>2</sup> ) |
|---------|---------|---------|-----------|---------|-------------------------|
| 0.00    | 0.00    | 0.00    | 0.00      | 0.063   | 3.52                    |
| 0.25    | 0.11    | 0.125   | 0.44      | 0.25    | 3.84                    |
| 0.50    | 0.46    | 0.375   | 1.40      | 0.50    | 4.00                    |
| 0.75    | 1.06    | 0.625   | 2.40      | 0.75    | 4.48                    |
| 1.00    | 1.94    | 0.875   | 3.52      | 1.06    | 4.91                    |
| 1.50    | 4.62    | 1.25    | 5.36      | 1.50    | 5.00                    |
| 2.00    | 8.55    | 1.75    | 7.86      | 2.00    | 5.24                    |
| 2.50    | 13.79   | 2.25    | 10.48     | 2.50    | 5.32                    |
| 3.00    | 20.36   | 2.75    | 13.14     | 3.00    | 5.52                    |
| 3.50    | 28.31   | 3.25    | 15.90     | 3.50    | 5.56                    |
| 4.00    | 37.65   | 3.75    | 18.68     | 4.00    | 5.52                    |
| 4.50    | 48.37   | 4.25    | 21.44     | 4.50    | 4.84                    |
| 5.00    | 60.30   | 4.75    | 23.86     | 5.00    | 4.12                    |
| 5.50    | 73.26   | 5.25    | 25.92     | 5.50    | 3.76                    |
| 6.00    | 87.16   | 5.75    | 27.80     |         |                         |



29. We call the location where the cars are initially next to each other  $x_0 = 0$ . The position of the first car can be written as  $x = x_0 + v_0 t + \frac{1}{2} a t^2 = 25.0t - \frac{1}{2}(2.0)t^2$ . The position of the second car can be written as  $x = x_0 + v_0 t + \frac{1}{2} a t^2 = \frac{1}{2}(2.0)t^2$ . We equate the two position equations and solve for the time.

$$25.0t - \frac{1}{2}(2.0)t^2 = \frac{1}{2}(2.0)t^2 \rightarrow 25.0t = 2.0t^2 \rightarrow t = 0 \text{ or } 12.5 \text{ s}$$

The value of 0 is the time when the cars were initially next to each other, so the “next” time they are next to each other is  $t = 12.5 \text{ s} \approx \boxed{13 \text{ s}}$ .

30. Slightly different answers may be obtained since the data comes from reading the graph.
- (a) The greatest velocity is found at the highest point on the graph, which is at  $t \approx 48 \text{ s}$ .
  - (b) The indication of a constant velocity on a velocity–time graph is a slope of 0, which occurs from  $t = 90 \text{ s}$  to  $t \approx 108 \text{ s}$ .
  - (c) The indication of a constant acceleration on a velocity–time graph is a constant slope, which occurs from  $t = 0 \text{ s}$  to  $t \approx 42 \text{ s}$ , again from  $t \approx 65 \text{ s}$  to  $t \approx 83 \text{ s}$ , and again from  $t = 90 \text{ s}$  to  $t \approx 108 \text{ s}$ .
  - (d) The magnitude of the acceleration is greatest when the magnitude of the slope is greatest, which occurs from  $t \approx 65 \text{ s}$  to  $t \approx 83 \text{ s}$ .

31. Slightly different answers may be obtained since the data comes from reading the graph. We assume that the short, nearly horizontal portions of the graph are the times that shifting is occurring, and those times are not counted as being “in” a certain gear.

- (a) The average acceleration in 2<sup>nd</sup> gear is given by  $\bar{a}_2 = \frac{\Delta v_2}{\Delta t_2} = \frac{24 \text{ m/s} - 14 \text{ m/s}}{8 \text{ s} - 4 \text{ s}} = 2.5 \text{ m/s}^2$ .
- (b) The average acceleration in 4<sup>th</sup> gear is given by  $\bar{a}_4 = \frac{\Delta v_4}{\Delta t_4} = \frac{44 \text{ m/s} - 37 \text{ m/s}}{27 \text{ s} - 16 \text{ s}} = 0.6 \text{ m/s}^2$ .

32. (a) The train’s constant speed is  $v_{\text{train}} = 5.0 \text{ m/s}$ , and the location of the empty box car as a function of time is given by  $x_{\text{train}} = v_{\text{train}}t = (5.0 \text{ m/s})t$ . The fugitive has  $v_0 = 0 \text{ m/s}$  and  $a = 1.4 \text{ m/s}^2$  until his final speed is  $6.0 \text{ m/s}$ . The elapsed time during the acceleration is  $t_{\text{acc}} = \frac{v - v_0}{a} = \frac{6.0 \text{ m/s}}{1.4 \text{ m/s}^2} = 4.286 \text{ s}$ . Let the origin be the location of the fugitive when he starts to run. The first possibility to consider is, “Can the fugitive catch the empty box car before he reaches his maximum speed?” During the fugitive’s acceleration, his location as a function of time is given by Eq. 2–12b,  $x_{\text{fugitive}} = x_0 + v_0t + \frac{1}{2}at^2 = 0 + 0 + \frac{1}{2}(1.4 \text{ m/s}^2)t^2$ . For him to catch the train, we must have  $x_{\text{train}} = x_{\text{fugitive}} \rightarrow (5.0 \text{ m/s})t = \frac{1}{2}(1.4 \text{ m/s}^2)t^2$ . The solutions of this are  $t = 0 \text{ s}$ ,  $7.1 \text{ s}$ . Thus the fugitive cannot catch the car during his  $4.286 \text{ s}$  of acceleration.

Now the equation of motion of the fugitive changes. After the  $4.286 \text{ s}$  of acceleration, he runs with a constant speed of  $6.0 \text{ m/s}$ . Thus his location is now given (for times  $t > 4.286 \text{ s}$ ) by the following.

$$x_{\text{fugitive}} = \frac{1}{2}(1.4 \text{ m/s}^2)(4.286 \text{ s})^2 + (6.0 \text{ m/s})(t - 4.286 \text{ s}) = (6.0 \text{ m/s})t - 12.86 \text{ m}$$

So now, for the fugitive to catch the train, we again set the locations equal.

$$x_{\text{train}} = x_{\text{fugitive}} \rightarrow (5.0 \text{ m/s})t = (6.0 \text{ m/s})t - 12.86 \text{ m} \rightarrow t = 12.86 \text{ s} \approx 13 \text{ s}$$

- (b) The distance traveled to reach the box car is given by the following.

$$x_{\text{fugitive}}(t = 12.86 \text{ s}) = (6.0 \text{ m/s})(12.86 \text{ s}) - 12.86 \text{ m} = 64 \text{ m}$$

33. The acceleration can be found from Eq. 2–12c.

$$v^2 = v_0^2 + 2a(x - x_0) \rightarrow a = \frac{v^2 - v_0^2}{2(x - x_0)} = \frac{0 - (26 \text{ m/s})^2}{2(88 \text{ m})} = -3.8 \text{ m/s}^2$$

34. The acceleration can be found from Eq. 2-12a.

$$v = v_0 + at \rightarrow a = \frac{v - v_0}{t} = \frac{0 - 28 \text{ m/s}}{6.3 \text{ s}} = \boxed{-4.4 \text{ m/s}^2}$$

35. By definition, the acceleration is  $a = \frac{v - v_0}{t} = \frac{22 \text{ m/s} - 13 \text{ m/s}}{6.5 \text{ s}} = 1.38 \text{ m/s}^2 \approx \boxed{1.4 \text{ m/s}^2}$ .

The distance of travel can be found from Eqs. 2-8 and 2-9.

$$x - x_0 = \bar{v}\Delta t = \frac{v_0 + v}{2} \Delta t = \frac{13 \text{ m/s} + 22 \text{ m/s}}{2} (6.5 \text{ s}) = 114 \text{ m} \approx \boxed{110 \text{ m}}$$

It can also be found from Eq. 2-12b.

$$x - x_0 = v_0 t + \frac{1}{2} a t^2 = (13 \text{ m/s})(6.5 \text{ s}) + \frac{1}{2} (1.38 \text{ m/s}^2)(6.5 \text{ s})^2 = 113.7 \text{ m} \approx 110 \text{ m}$$

It can also be found from Eq. 2-12c.

$$v^2 = v_0^2 + 2a(x - x_0) \rightarrow x - x_0 = \frac{v^2 - v_0^2}{2a} = \frac{(22 \text{ m/s})^2 - (13 \text{ m/s})^2}{2(1.38 \text{ m/s}^2)} = 114.1 \text{ m} \approx 110 \text{ m}$$

There are slight differences in the answers because of rounding the acceleration.

36. The sprinter starts from rest. The average acceleration is found from Eq. 2-12c.

$$v^2 = v_0^2 + 2a(x - x_0) \rightarrow a = \frac{v^2 - v_0^2}{2(x - x_0)} = \frac{(11.5 \text{ m/s})^2 - 0}{2(18.0 \text{ m})} = 3.674 \text{ m/s}^2 \approx \boxed{3.67 \text{ m/s}^2}$$

Her elapsed time is found by solving Eq. 2-12a for time.

$$v = v_0 + at \rightarrow t = \frac{v - v_0}{a} = \frac{11.5 \text{ m/s} - 0}{3.674 \text{ m/s}^2} = \boxed{3.13 \text{ s}}$$

37. The words “slowing down uniformly” imply that the car has a constant acceleration. The distance of travel is found from combining Eqs. 2-8 and 2-9.

$$x - x_0 = \frac{v_0 + v}{2} t = \left( \frac{28.0 \text{ m/s} + 0 \text{ m/s}}{2} \right) (8.60 \text{ sec}) = \boxed{1.20 \times 10^2 \text{ m}}$$

38. The final velocity of the truck is zero. The initial velocity is found from Eq. 2-12c with  $v = 0$  and solving for  $v_0$ . Note that the acceleration is negative.

$$v^2 = v_0^2 + 2a(x - x_0) \rightarrow v_0 = \sqrt{v^2 - 2a(x - x_0)} = \sqrt{0 - 2(-6.00 \text{ m/s}^2)(45 \text{ m})} = \boxed{23 \text{ m/s}}$$

39. For the baseball,  $v_0 = 0$ ,  $x - x_0 = 3.5 \text{ m}$ , and the final speed of the baseball (during the throwing motion) is  $v = 43 \text{ m/s}$ . The acceleration is found from Eq. 2-12c.

$$v^2 = v_0^2 + 2a(x - x_0) \rightarrow a = \frac{v^2 - v_0^2}{2(x - x_0)} = \frac{(43 \text{ m/s})^2 - 0}{2(3.5 \text{ m})} = 264 \text{ m/s}^2 \approx \boxed{260 \text{ m/s}^2}$$

40. The final velocity of the driver is zero. The acceleration is found from Eq. 2-12c with  $v = 0$  and solving for  $a$ .

$$a = \frac{v^2 - v_0^2}{2(x - x_0)} = \frac{0 - \left[ (95 \text{ km/h}) \left( \frac{1000 \text{ m}}{1 \text{ km}} \right) \left( \frac{1 \text{ h}}{3600 \text{ s}} \right) \right]^2}{2(0.80 \text{ m})} = -435.2 \text{ m/s}^2$$

Converting to “g’s”:  $|a| = \frac{435.2 \text{ m/s}^2}{(9.80 \text{ m/s}^2)/g} = \boxed{44 g's}$ .

41. (a) The final velocity of the car is 0. The distance is found from Eq. 2-12c with an acceleration of  $a = -0.50 \text{ m/s}^2$  and an initial velocity of 85 km/h.

$$x - x_0 = \frac{v^2 - v_0^2}{2a} = \frac{0 - \left[ (85 \text{ km/h}) \left( \frac{1000 \text{ m}}{1 \text{ km}} \right) \left( \frac{1 \text{ h}}{3600 \text{ s}} \right) \right]^2}{2(-0.50 \text{ m/s}^2)} = 557 \text{ m} \approx \boxed{560 \text{ m}}$$

- (b) The time to stop is found from Eq. 2-12a.

$$t = \frac{v - v_0}{a} = \frac{0 - \left[ (85 \text{ km/h}) \left( \frac{1000 \text{ m}}{1 \text{ km}} \right) \left( \frac{1 \text{ h}}{3600 \text{ s}} \right) \right]}{(-0.50 \text{ m/s}^2)} = 47.22 \text{ s} \approx \boxed{47 \text{ s}}$$

- (c) Take  $x_0 = x(t = 0) = 0 \text{ m}$ . Use Eq. 2-12b, with  $a = -0.50 \text{ m/s}^2$  and an initial velocity of 85 km/h. The first second is from  $t = 0 \text{ s}$  to  $t = 1 \text{ s}$ , and the fifth second is from  $t = 4 \text{ s}$  to  $t = 5 \text{ s}$ .

$$x(0) = 0 ; x(1) = 0 + (85 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) (1 \text{ s}) + \frac{1}{2} (-0.50 \text{ m/s}^2) (1 \text{ s})^2 = 23.36 \text{ m} \rightarrow$$

$$x(1) - x(0) = \boxed{23 \text{ m}}$$

$$x(4) = 0 + (85 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) (4 \text{ s}) + \frac{1}{2} (-0.50 \text{ m/s}^2) (4 \text{ s})^2 = 90.44 \text{ m}$$

$$x(5) = 0 + (85 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) (5 \text{ s}) + \frac{1}{2} (-0.50 \text{ m/s}^2) (5 \text{ s})^2 = 111.81 \text{ m}$$

$$x(5) - x(4) = 111.81 \text{ m} - 90.44 \text{ m} = 21.37 \text{ m} \approx \boxed{21 \text{ m}}$$

42. The origin is the location of the car at the beginning of the reaction time. The initial speed of the car is  $(95 \text{ km/h}) \left( \frac{1000 \text{ m}}{1 \text{ km}} \right) \left( \frac{1 \text{ h}}{3600 \text{ s}} \right) = 26.39 \text{ m/s}$ . The location where the brakes are applied is found from the equation for motion at constant velocity.

$$x_0 = v_0 t_R = (26.39 \text{ m/s})(0.40 \text{ s}) = 10.56 \text{ m}$$

This is now the starting location for the application of the brakes. In each case, the final speed is 0.

- (a) Solve Eq. 2-12c for the final location.

$$v^2 = v_0^2 + 2a(x - x_0) \rightarrow$$

$$x = x_0 + \frac{v^2 - v_0^2}{2a} = 10.56 \text{ m} + \frac{0 - (26.39 \text{ m/s})^2}{2(-2.5 \text{ m/s}^2)} = 149.84 \text{ m} \approx \boxed{150 \text{ m}}$$

- (b) Solve Eq. 2-12c for the final location with the second acceleration.

$$x = x_0 + \frac{v^2 - v_0^2}{2a} = 10.56 \text{ m} + \frac{0 - (26.39 \text{ m/s})^2}{2(-5.5 \text{ m/s}^2)} = \boxed{74 \text{ m}}$$

43. Calculate the distance that the car travels during the reaction time and the deceleration.

$$\Delta x_1 = v_0 \Delta t = (18.0 \text{ m/s})(0.380 \text{ s}) = 6.84 \text{ m}$$

$$v^2 = v_0^2 + 2a\Delta x_2 \rightarrow \Delta x_2 = \frac{v^2 - v_0^2}{2a} = \frac{0 - (18.0 \text{ m/s})^2}{2(-3.65 \text{ m/s}^2)} = 44.38 \text{ m}$$

$$\Delta x = 6.84 \text{ m} + 44.4 \text{ m} = 51.22 \text{ m} \quad (\text{only 3 significant figures})$$

Since she is only 24.0 m from the intersection, she will NOT be able to stop in time. She will be 27.2 m past the intersection.

44. The average velocity is defined by Eq. 2-2,
- $\bar{v} = \frac{\Delta x}{\Delta t} = \frac{x - x_0}{t}$
- . Compare this expression to

Eq. 2-12d,  $\bar{v} = \frac{1}{2}(v + v_0)$ . A relation for the velocity is found by integrating the expression for the acceleration, since the acceleration is the derivative of the velocity. Assume the velocity is  $v_0$  at time  $t = 0$ .

$$a = A + Bt = \frac{dv}{dt} \rightarrow dv = (A + Bt) dt \rightarrow \int_{v_0}^v dv = \int_0^t (A + Bt) dt \rightarrow v = v_0 + At + \frac{1}{2} Bt^2$$

Find an expression for the position by integrating the velocity, assuming that  $x = x_0$  at time  $t = 0$ .

$$v = v_0 + At + \frac{1}{2} Bt^2 = \frac{dx}{dt} \rightarrow dx = (v_0 + At + \frac{1}{2} Bt^2) dt \rightarrow$$

$$\int_{x_0}^x dx = \int_0^t (v_0 + At + \frac{1}{2} Bt^2) dt \rightarrow x - x_0 = v_0 t + \frac{1}{2} At^2 + \frac{1}{6} Bt^3$$

Compare  $\frac{x - x_0}{t}$  to  $\frac{1}{2}(v + v_0)$ .

$$\bar{v} = \frac{x - x_0}{t} = \frac{v_0 t + \frac{1}{2} At^2 + \frac{1}{6} Bt^3}{t} = v_0 + \frac{1}{2} At + \frac{1}{6} Bt^2$$

$$\frac{1}{2}(v + v_0) = \frac{v_0 + v_0 + At + \frac{1}{2} Bt^2}{2} = v_0 + \frac{1}{2} At + \frac{1}{4} Bt^2$$

They are different, so  $\boxed{\bar{v} \neq \frac{1}{2}(v + v_0)}$ .

45. Use the information for the first 180 m to find the acceleration, and the information for the full motion to find the final velocity. For the first segment, the train has
- $v_0 = 0 \text{ m/s}$
- ,
- $v_1 = 18 \text{ m/s}$
- , and a displacement of
- $x_1 - x_0 = 180 \text{ m}$
- . Find the acceleration from Eq. 2-12c.

$$v_1^2 = v_0^2 + 2a(x_1 - x_0) \rightarrow a = \frac{v_1^2 - v_0^2}{2(x_1 - x_0)} = \frac{(18 \text{ m/s})^2 - 0}{2(180 \text{ m})} = 0.90 \text{ m/s}^2$$

Find the speed of the train after it has traveled the total distance (total displacement of  $x_2 - x_0 = 180 \text{ m} + 85 \text{ m} = 265 \text{ m}$ ) using Eq. 2-12c.

$$v_2^2 = v_0^2 + 2a(x_2 - x_0) \rightarrow v_2 = \sqrt{v_0^2 + 2a(x_2 - x_0)} = \sqrt{2(0.90 \text{ m/s}^2)(265 \text{ m})} = \boxed{22 \text{ m/s}}$$

46. Calculate the acceleration from the velocity–time data using Eq. 2-12a, and then use Eq. 2-12b to calculate the displacement at  $t = 2.0 \text{ s}$  and  $t = 6.0 \text{ s}$ . The initial velocity is  $v_0 = 85 \text{ m/s}$ .

$$a = \frac{v - v_0}{t} = \frac{162 \text{ m/s} - 85 \text{ m/s}}{10.0 \text{ s}} = 7.7 \text{ m/s}^2 \quad x = x_0 + v_0 t + \frac{1}{2} a t^2 \rightarrow$$

$$\begin{aligned} x(7.0 \text{ s}) - x(2.0 \text{ s}) &= \left[ \left( x_0 + v_0(7.0 \text{ s}) + \frac{1}{2} a(7.0 \text{ s})^2 \right) - \left( x_0 + v_0(2.0 \text{ s}) + \frac{1}{2} a(2.0 \text{ s})^2 \right) \right] \\ &= v_0(7.0 \text{ s} - 2.0 \text{ s}) + \frac{1}{2} a \left[ (7.0 \text{ s})^2 - (2.0 \text{ s})^2 \right] = (85 \text{ m/s})(5.0 \text{ s}) + \frac{1}{2} (7.7 \text{ m/s}^2)(45 \text{ s}^2) \\ &= 598.25 \text{ m} \approx \boxed{6.0 \times 10^2 \text{ m}} \end{aligned}$$

47. During the final part of the race, the runner must have a displacement of 1200 m in a time of 180 s (3.0 min). Assume that the starting speed for the final part is the same as the average speed thus far.

$$\bar{v} = \frac{\Delta x}{\Delta t} = \frac{8800 \text{ m}}{(27 \times 60) \text{ s}} = 5.432 \text{ m/s} = v_0$$

The runner will accomplish this by accelerating from speed  $v_0$  to speed  $v$  for  $t$  seconds, covering a distance  $d_1$ , and then running at a constant speed of  $v$  for  $(180 - t)$  seconds, covering a distance  $d_2$ . We have these relationships from Eq. 2-12a and Eq. 2-12b.

$$\begin{aligned} v &= v_0 + at & d_1 &= v_0 t + \frac{1}{2} a t^2 & d_2 &= v(180 - t) = (v_0 + at)(180 - t) \\ 1200 \text{ m} &= d_1 + d_2 = v_0 t + \frac{1}{2} a t^2 + (v_0 + at)(180 - t) \rightarrow 1200 \text{ m} = 180 v_0 + 180 a t - \frac{1}{2} a t^2 \rightarrow \\ 1200 \text{ m} &= (180 \text{ s})(5.432 \text{ m/s}) + (180 \text{ s})(0.20 \text{ m/s}^2) t - \frac{1}{2} (0.20 \text{ m/s}^2) t^2 \rightarrow \\ 0.10 t^2 - 36 t + 222.24 &= 0 \rightarrow t = \frac{36 \pm \sqrt{36^2 - 4(0.10)(222.24)}}{2(0.10)} = 353.7 \text{ s}, 6.28 \text{ s} \end{aligned}$$

Since we must have  $t < 180 \text{ s}$ , the solution is  $\boxed{t = 6.3 \text{ s}}$ .

48. For the runners to cross the finish line side-by-side means they must both reach the finish line in the same amount of time from their current positions. Take Mary's current location as the origin. Use Eq. 2-12b.

$$\begin{aligned} \text{For Sally: } 22 &= 5.0 + 5.0 t + \frac{1}{2} (-0.40) t^2 \rightarrow t^2 - 25 t + 85 = 0 \rightarrow \\ t &= \frac{25 \pm \sqrt{25^2 - 4(85)}}{2} = 4.059 \text{ s}, 20.94 \text{ s} \end{aligned}$$

The first time is the time she first crosses the finish line, and so it is the time to be used for the problem. Now find Mary's acceleration so that she crosses the finish line in that same amount of time.

$$\text{For Mary: } 22 = 0 + 4t + \frac{1}{2}at^2 \rightarrow a = \frac{22 - 4t}{\frac{1}{2}t^2} = \frac{22 - 4(4.059)}{\frac{1}{2}(4.059)^2} = \boxed{0.70 \text{ m/s}^2}$$

49. Define the origin to be the location where the speeder passes the police car. Start a timer at the instant that the speeder passes the police car, and find another time that both cars have the same displacement from the origin.

For the speeder, traveling with a constant speed, the displacement is given by the following.

$$\Delta x_s = v_s t = (135 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) (t) = (37.5 t) \text{ m}$$

For the police car, the displacement is given by two components. The first part is the distance traveled at the initially constant speed during the 1 second of reaction time.

$$\Delta x_{p1} = v_{op} (1.00 \text{ s}) = (95 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) (1.00 \text{ s}) = 26.39 \text{ m}$$

The second part of the police car's displacement is that which occurs during the accelerated motion, which lasts for  $(t - 1.00) \text{ s}$ . So this second part of the police car displacement, using Eq. 2-12b, is given as follows. Note that this part of the displacement is NOT VALID for  $t < 1.00 \text{ s}$ .

$$\Delta x_{p2} = v_{op} (t - 1.00) + \frac{1}{2} a_p (t - 1.00)^2 = \left[ (26.39 \text{ m/s})(t - 1.00) + \frac{1}{2} (2.60 \text{ m/s}^2)(t - 1.00)^2 \right] \text{ m}$$

So the total police car displacement is:

$$\Delta x_p = \Delta x_{p1} + \Delta x_{p2} = (26.39 + 26.39(t - 1.00) + 1.30(t - 1.00)^2) \text{ m}$$

Now set the two displacements equal, and solve for the time.

$$26.39 + 26.39(t - 1.00) + 1.30(t - 1.00)^2 = 37.5 t \rightarrow t^2 - 10.55t + 1.00 = 0$$

$$t = \frac{10.55 \pm \sqrt{(10.55)^2 - 4.00}}{2} = 9.57 \times 10^{-2} \text{ s}, \boxed{10.5 \text{ s}}$$

The first answer from the quadratic formula is a "fake" answer, because the equation for the police car's displacement while accelerating, which was used to find that solution, was not valid for times  $t < 1.00 \text{ s}$ . Thus we may ignore that answer. The answer of 10.5 s is the time for the police car to overtake the speeder.

As a check on the answer, the speeder travels  $\Delta x_s = (37.5 \text{ m/s})(10.5 \text{ s}) = 394 \text{ m}$ , and the police car travels  $\Delta x_p = [26.39 + 26.39(9.5) + 1.30(9.5)^2] \text{ m} = 394 \text{ m}$ .

50. Define the origin to be the location where the speeder passes the police car. Start a timer at the instant that the speeder passes the police car. Both cars have the same displacement 8.00 s after the initial passing by the speeder. But the police car only is accelerating for 7.00 s.

For the speeder, traveling with a constant speed, the displacement is given by  $\Delta x_s = v_s t = (8.00 v_s) \text{ m}$ .

For the police car, the displacement is given by two components. The first part is the distance traveled at the initially constant speed during the 1.00 s of reaction time.

$$\Delta x_{p1} = v_{op} (1.00 \text{ s}) = (95 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) (1.00 \text{ s}) = 26.39 \text{ m}$$

The second part of the police car displacement is that during the accelerated motion, which lasts for 7.00 s. So this second part of the police car displacement, using Eq. 2-12b, is given by the following.

$$\Delta x_{p2} = v_{0p}(7.00 \text{ s}) + \frac{1}{2}a_p(7.00 \text{ s})^2 = (26.39 \text{ m/s})(7.00 \text{ s}) + \frac{1}{2}(2.60 \text{ m/s}^2)(7.00 \text{ s})^2 = 248.43 \text{ m}$$

Thus the total police car displacement is  $\Delta x_p = \Delta x_{p1} + \Delta x_{p2} = (26.39 + 248.43) \text{ m} = 274.82 \text{ m}$ .

Now set the two displacements equal, and solve for the speeder's velocity.

$$(8.00v_s) \text{ m} = 274.82 \text{ m} \rightarrow v_s = 34.35 \text{ m/s} = (34.35 \text{ m/s}) \left( \frac{3.6 \text{ km/h}}{1 \text{ m/s}} \right) = \boxed{124 \text{ km/h}}$$

51. From the given information, we can break the race up into three segments:

Segment # 1: Time of 0.15 seconds, no displacement.

Segment # 2: Starting speed of 0, final speed  $v$ , constant acceleration  $a$ , displacement 30.0 m, elapsed time  $t_2$ . Thus  $v = at_2$  and  $30 \text{ m} = \frac{1}{2}at_2^2$ .

Segment # 3: Constant velocity  $v$ , displacement of 370 m, elapsed time  $t_3$ . Thus  $370 \text{ m} = vt_3$ .

We also know that  $t_2 + t_3 = 54.85 \text{ s}$ . So we have 4 relationships defining the 4 unknowns of  $v$ ,  $a$ ,  $t_2$ , and  $t_3$ . We solve that system of 4 equations.

$$v = at_2 ; 30 = \frac{1}{2}at_2^2 ; 370 = vt_3 ; t_2 + t_3 = 54.85 \quad \text{Substitute the 1}^{\text{st}} \text{ equation into the 3}^{\text{rd}}.$$

$$30 = \frac{1}{2}at_2^2 ; 370 = at_2t_3 ; t_2 + t_3 = 54.85 \quad \text{Divide the 2}^{\text{nd}} \text{ equation by the 1}^{\text{st}}.$$

$$\frac{370}{30} = \frac{at_2t_3}{\frac{1}{2}at_2^2} = \frac{2t_3}{t_2} ; t_2 + t_3 = 54.85 \quad \text{Substitute the 1}^{\text{st}} \text{ equation into the 2}^{\text{nd}}.$$

$$\frac{370}{30} = \frac{2t_3}{t_2} \rightarrow t_2 = \frac{60}{370}t_3 ; \frac{60}{370}t_3 + t_3 = 54.85 \quad \text{Solve for } t_3.$$

$$\frac{60}{370}t_3 + t_3 = 1.162t_3 = 54.85 \rightarrow t_3 = \frac{54.85}{1.162} = 47.20 \text{ s} \rightarrow t_2 = 54.85 - t_3 = 7.65 \text{ s}$$

$$v = \frac{370 \text{ m}}{t_3} = \frac{370 \text{ m}}{47.20 \text{ s}} = 7.839 \text{ m/s} ; a = \frac{v}{t_2} = \frac{7.839 \text{ m/s}}{7.65 \text{ s}} = 1.025 \text{ m/s}^2$$

The requested results are  $\boxed{v = 7.8 \text{ m/s} ; a = 1.0 \text{ m/s}^2}$ .

52. Choose downward to be the positive direction, and take  $y_0 = 0$  at the top of the cliff. The initial velocity is  $v_0 = 0$ , and the acceleration is  $a = 9.80 \text{ m/s}^2$ . The displacement is found from Eq. 2-12b, with  $x$  replaced by  $y$ .

$$y = y_0 + v_0t + \frac{1}{2}at^2 \rightarrow y - 0 = 0 + \frac{1}{2}(9.80 \text{ m/s}^2)(3.25 \text{ s})^2 \rightarrow y = \boxed{51.8 \text{ m}}$$

53. Choose downward to be the positive direction, and take  $y_0 = 0$  to be at the top of the Empire State Building. The initial velocity is  $v_0 = 0$ , and the acceleration is  $a = 9.80 \text{ m/s}^2$ .

(a) The elapsed time can be found from Eq. 2-12b, with  $x$  replaced by  $y$ .

$$y - y_0 = v_0t + \frac{1}{2}at^2 \rightarrow t = \sqrt{\frac{2y}{a}} = \sqrt{\frac{2(380 \text{ m})}{9.80 \text{ m/s}^2}} = 8.806 \text{ s} \approx \boxed{8.8 \text{ s}}$$

(b) The final velocity can be found from Eq. 2-12a.

$$v = v_0 + at = 0 + (9.80 \text{ m/s}^2)(8.806 \text{ s}) = \boxed{86 \text{ m/s}}$$

54. Choose downward to be the positive direction. The initial velocity is  $v_0 = 0$ , the final velocity is

$$v = (55 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) = 15.28 \text{ m/s}, \text{ and the acceleration is } a = 9.80 \text{ m/s}^2. \text{ Solve Eq. 2-12a}$$

for the time.

$$v = v_0 + at \rightarrow t = \frac{v - v_0}{a} = \frac{15.28 \text{ m/s} - 0}{9.80 \text{ m/s}^2} = \boxed{1.6 \text{ s}}$$

55. Choose upward to be the positive direction, and take  $y_0 = 0$  to be the height from which the ball was thrown. The acceleration is  $a = -9.80 \text{ m/s}^2$ . The displacement upon catching the ball is 0, assuming it was caught at the same height from which it was thrown. The starting speed can be found from Eq. 2-12b, with  $x$  replaced by  $y$ .

$$y = y_0 + v_0 t + \frac{1}{2} at^2 = 0 \rightarrow$$

$$v_0 = \frac{y - y_0 - \frac{1}{2} at^2}{t} = -\frac{1}{2} at = -\frac{1}{2} (-9.80 \text{ m/s}^2)(2.6 \text{ s}) = 12.74 \text{ m/s} \approx \boxed{13 \text{ m/s}}$$

The height can be calculated from Eq. 2-12c, with a final velocity of  $v = 0$  at the top of the path.

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow y = y_0 + \frac{v^2 - v_0^2}{2a} = 0 + \frac{0 - (12.74 \text{ m/s})^2}{2(-9.80 \text{ m/s}^2)} = \boxed{8.3 \text{ m}}$$

56. Choose upward to be the positive direction, and take  $y_0 = 0$  to be at the height where the ball was hit. For the upward path,  $v_0 = 22 \text{ m/s}$ ,  $v = 0$  at the top of the path, and  $a = -9.80 \text{ m/s}^2$ .

(a) The displacement can be found from Eq. 2-12c, with  $x$  replaced by  $y$ .

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow y = y_0 + \frac{v^2 - v_0^2}{2a} = 0 + \frac{0 - (22 \text{ m/s})^2}{2(-9.80 \text{ m/s}^2)} = \boxed{25 \text{ m}}$$

(b) The time of flight can be found from Eq. 2-12b, with  $x$  replaced by  $y$ , using a displacement of 0 for the displacement of the ball returning to the height from which it was hit.

$$y = y_0 + v_0 t + \frac{1}{2} at^2 = 0 \rightarrow t(v_0 + \frac{1}{2} at) = 0 \rightarrow$$

$$t = 0, t = \frac{2v_0}{-a} = \frac{2(22 \text{ m/s})}{-9.80 \text{ m/s}^2} = \boxed{4.5 \text{ s}}$$

The result of  $t = 0 \text{ s}$  is the time for the original displacement of zero (when the ball was hit), and the result of  $t = 4.5 \text{ s}$  is the time to return to the original displacement. Thus the answer is  $t = 4.5$  seconds.

(c) This is an estimate primarily because the effects of the air have been ignored. There is a non-trivial amount of air effect on a baseball as it moves through the air – that's why pitches like the "curve ball" work, for example. So ignoring the effects of air make this an estimate. Another effect is that the problem says "almost" straight up, but the problem was solved as if the initial velocity was perfectly upwards. Finally, we assume that the ball was caught at the same height as which it was hit. That was not stated in the problem either, so that is an estimate.

57. Choose downward to be the positive direction, and take  $y_0 = 0$  to be at the maximum height of the kangaroo. Consider just the downward motion of the kangaroo. Then the displacement is  $y = 1.45$  m, the acceleration is  $a = 9.80$  m/s<sup>2</sup>, and the initial velocity is  $v_0 = 0$  m/s. Use Eq. 2-12b to calculate the time for the kangaroo to fall back to the ground. The total time is then twice the falling time.

$$y = y_0 + v_0 t + \frac{1}{2} a t^2 = 0 \rightarrow y = \frac{1}{2} a t^2 \rightarrow t_{\text{fall}} = \sqrt{\frac{2y}{a}} \rightarrow$$

$$t_{\text{total}} = 2\sqrt{\frac{2y}{a}} = 2\sqrt{\frac{2(1.45 \text{ m})}{(9.80 \text{ m/s}^2)}} = \boxed{1.09 \text{ s}}$$

58. Choose upward to be the positive direction, and take  $y_0 = 0$  to be at the floor level, where the jump starts. For the upward path,  $y = 1.2$  m,  $v = 0$  at the top of the path, and  $a = -9.80$  m/s<sup>2</sup>.

- (a) The initial speed can be found from Eq. 2-12c, with  $x$  replaced by  $y$ .

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow$$

$$v_0 = \sqrt{v^2 - 2a(y - y_0)} = \sqrt{-2ay} = \sqrt{-2(-9.80 \text{ m/s}^2)(1.2 \text{ m})} = 4.8497 \text{ m/s} \approx \boxed{4.8 \text{ m/s}}$$

- (b) The time of flight can be found from Eq. 2-12b, with  $x$  replaced by  $y$ , using a displacement of 0 for the displacement of the jumper returning to the original height.

$$y = y_0 + v_0 t + \frac{1}{2} a t^2 = 0 \rightarrow t(v_0 + \frac{1}{2} a t) = 0 \rightarrow$$

$$t = 0, t = \frac{2v_0}{-a} = \frac{2(4.897 \text{ m/s})}{-9.80 \text{ m/s}^2} = \boxed{0.99 \text{ s}}$$

The result of  $t = 0$  s is the time for the original displacement of zero (when the jumper started to jump), and the result of  $t = 0.99$  s is the time to return to the original displacement. Thus the answer is  $t = 0.99$  seconds.

59. Choose upward to be the positive direction, and  $y_0 = 0$  to be the height from which the stone is thrown. We have  $v_0 = 18.0$  m/s,  $a = -9.80$  m/s<sup>2</sup>, and  $y - y_0 = 11.0$  m.

- (a) The velocity can be found from Eq. 2-11c, with  $x$  replaced by  $y$ .

$$v^2 = v_0^2 + 2a(y - y_0) = 0 \rightarrow$$

$$v = \pm \sqrt{v_0^2 + 2ay} = \pm \sqrt{(18.0 \text{ m/s})^2 + 2(-9.80 \text{ m/s}^2)(11.0 \text{ m})} = \pm 10.4 \text{ m/s}$$

Thus the speed is  $\boxed{|v| = 10.4 \text{ m/s}}$ .

- (b) The time to reach that height can be found from Eq. 2-12b.

$$y = y_0 + v_0 t + \frac{1}{2} a t^2 \rightarrow t^2 + \frac{2(18.0 \text{ m/s})}{-9.80 \text{ m/s}^2} t + \frac{2(-11.0 \text{ m})}{-9.80 \text{ m/s}^2} = 0 \rightarrow$$

$$t^2 - 3.6735t + 2.245 = 0 \rightarrow t = \frac{3.6735 \pm \sqrt{(3.6735)^2 - 4(2.2449)}}{2} = \boxed{t = 2.90 \text{ s}, 0.774 \text{ s}}$$

- (c) There are two times at which the object reaches that height – once on the way up ( $t = 0.774$  s), and once on the way down ( $t = 2.90$  s).

60. Choose downward to be the positive direction, and take  $y_0 = 0$  to be the height from which the object is released. The initial velocity is  $v_0 = 0$ , and the acceleration is  $a = g$ . Then we can calculate the position as a function of time from Eq. 2-12b, with  $x$  replaced by  $y$ , as  $y(t) = \frac{1}{2}gt^2$ . At the end of each second, the position would be as follows.

$$y(0) = 0 ; \quad y(1) = \frac{1}{2}g ; \quad y(2) = \frac{1}{2}g(2)^2 = 4y(1) ; \quad y(3) = \frac{1}{2}g(3)^2 = 9y(1)$$

The distance traveled during each second can be found by subtracting two adjacent position values from the above list.

$$d(1) = y(1) - y(0) = y(1) ; \quad d(2) = y(2) - y(1) = 3y(1) ; \quad d(3) = y(3) - y(2) = 5y(1)$$

We could do this in general. Let  $n$  be a positive integer, starting with 0.

$$y(n) = \frac{1}{2}gn^2 \quad y(n+1) = \frac{1}{2}g(n+1)^2$$

$$d(n+1) = y(n+1) - y(n) = \frac{1}{2}g(n+1)^2 - \frac{1}{2}gn^2 = \frac{1}{2}g((n+1)^2 - n^2) \\ = \frac{1}{2}g(n^2 + 2n + 1 - n^2) = \frac{1}{2}g(2n+1)$$

The value of  $(2n+1)$  is always odd, in the sequence 1, 3, 5, 7, ....

61. Choose downward to be the positive direction, and the origin to be at the location of the plane. The parachutist has  $v_0 = 0$ ,  $a = g = 9.80 \text{ m/s}^2$ , and will have  $y - y_0 = 3800 \text{ m} - 450 \text{ m} = 3350 \text{ m}$  when she pulls the ripcord. Eq. 2-12b, with  $x$  replaced by  $y$ , is used to find the time when she pulls the ripcord.

$$y = y_0 + v_0t + \frac{1}{2}at^2 \rightarrow t = \sqrt{2(y - y_0)/a} = \sqrt{2(3350 \text{ m})/(9.80 \text{ m/s}^2)} = 26.147 \text{ s} \approx \boxed{26.1 \text{ s}}$$

The speed is found from Eq. 2-12a.

$$v = v_0 + at = 0 + (9.80 \text{ m/s}^2)(26.147 \text{ s}) = 256.24 \text{ m/s} \approx \boxed{256 \text{ m/s}}$$

$$(256.24 \text{ m/s}) \left( \frac{3.6 \text{ km/h}}{1 \text{ m/s}} \right) \approx \boxed{922 \text{ km/h}}$$

This is well over 550 miles per hour!

62. Choose downward to be the positive direction, and  $y_0 = 0$  to be at the start of the pelican's dive. The pelican has an initial velocity is  $v_0 = 0$ , an acceleration of  $a = g$ , and a final location of  $y = 16.0 \text{ m}$ . Find the total time of the pelican's dive from Eq. 2-12b, with  $x$  replaced by  $y$ .

$$y = y_0 + v_0t + \frac{1}{2}at^2 \rightarrow y = 0 + 0 + \frac{1}{2}at^2 \rightarrow t_{\text{dive}} = \sqrt{\frac{2y}{a}} = \sqrt{\frac{2(16.0 \text{ m})}{9.80 \text{ m/s}^2}} = 1.81 \text{ s}.$$

The fish can take evasive action if he sees the pelican at a time of  $1.81 \text{ s} - 0.20 \text{ s} = 1.61 \text{ s}$  into the dive. Find the location of the pelican at that time from Eq. 2-12b.

$$y = y_0 + v_0t + \frac{1}{2}at = 0 + 0 + \frac{1}{2}(9.80 \text{ m/s}^2)(1.61 \text{ s})^2 = 12.7 \text{ m}$$

Thus the fish must spot the pelican at a minimum height from the surface of the water of  $16.0 \text{ m} - 12.7 \text{ m} = \boxed{3.3 \text{ m}}$ .

63. Choose upward to be the positive direction, and  $y_0 = 0$  to be at the throwing location of the stone. The initial velocity is  $v_0 = 15.5 \text{ m/s}$ , the acceleration is  $a = -9.80 \text{ m/s}^2$ , and the final location is  $y = -75 \text{ m}$ .

(a) Using Eq. 2-12b and substituting  $y$  for  $x$ , we have the following.

$$y = y_0 + v_0 t + \frac{1}{2} a t^2 \rightarrow (4.9 \text{ m/s}^2) t^2 - (15.5 \text{ m/s}) t - 75 \text{ m} = 0 \rightarrow$$

$$t = \frac{15.5 \pm \sqrt{(15.5)^2 - 4(4.9)(-75)}}{2(4.9)} = 5.802 \text{ s}, -2.638 \text{ s}$$

The positive answer is the physical answer:  $t = 5.80 \text{ s}$ .

(b) Use Eq. 2-12a to find the velocity just before hitting.

$$v = v_0 + at = 15.5 \text{ m/s} + (-9.80 \text{ m/s}^2)(5.802 \text{ s}) = -41.4 \text{ m/s} \rightarrow |v| = 41.4 \text{ m/s}.$$

(c) The total distance traveled will be the distance up plus the distance down. The distance down will be 75 m more than the distance up. To find the distance up, use the fact that the speed at the top of the path will be 0. Then using Eq. 2-12c we have the following.

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow y = y_0 + \frac{v^2 - v_0^2}{2a} = 0 + \frac{0 - (15.5 \text{ m/s})^2}{2(-9.80 \text{ m/s}^2)} = 12.26 \text{ m}.$$

Thus the distance up is 12.26 m, the distance down is 87.26 m, and the total distance traveled is  $99.5 \text{ m}$ .

64. (a) Choose upward to be the positive direction, and  $y_0 = 0$  at the ground. The rocket has  $v_0 = 0$ ,  $a = 3.2 \text{ m/s}^2$ , and  $y = 725 \text{ m}$  when it runs out of fuel. Find the velocity of the rocket when it runs out of fuel from Eq. 2-12c, with  $x$  replaced by  $y$ .

$$v_{725 \text{ m}}^2 = v_0^2 + 2a(y - y_0) \rightarrow$$

$$v_{725 \text{ m}} = \pm \sqrt{v_0^2 + 2a(y - y_0)} = \pm \sqrt{0 + 2(3.2 \text{ m/s}^2)(725 \text{ m})} = 68.12 \text{ m/s} \approx 68 \text{ m/s}$$

The positive root is chosen since the rocket is moving upwards when it runs out of fuel.

(b) The time to reach the 725 m location can be found from Eq. 2-12a.

$$v_{725 \text{ m}} = v_0 + at_{725 \text{ m}} \rightarrow t_{725 \text{ m}} = \frac{v_{725 \text{ m}} - v_0}{a} = \frac{68.12 \text{ m/s} - 0}{3.2 \text{ m/s}^2} = 21.29 \text{ s} \approx 21 \text{ s}$$

(c) For this part of the problem, the rocket will have an initial velocity  $v_0 = v_{725 \text{ m}} = 68.12 \text{ m/s}$ , an acceleration of  $a = -9.80 \text{ m/s}^2$ , and a final velocity of  $v = 0$  at its maximum altitude. The altitude reached from the out-of-fuel point can be found from Eq. 2-12c.

$$v^2 = v_{725 \text{ m}}^2 + 2a(y - 725 \text{ m}) \rightarrow$$

$$y_{\text{max}} = 725 \text{ m} + \frac{0 - v_{725 \text{ m}}^2}{2a} = 725 \text{ m} + \frac{-(68.12 \text{ m/s})^2}{2(-9.80 \text{ m/s}^2)} = 725 \text{ m} + 237 \text{ m} = 962 \text{ m} \approx 960 \text{ m}$$

(d) The time for the “coasting” portion of the flight can be found from Eq. 2-12a.

$$v = v_{725 \text{ m}} + at_{\text{coast}} \rightarrow t_{\text{coast}} = \frac{v - v_{725 \text{ m}}}{a} = \frac{0 - 68.12 \text{ m/s}}{-9.80 \text{ m/s}^2} = 6.95 \text{ s}$$

Thus the total time to reach the maximum altitude is  $t = 21.29 \text{ s} + 6.95 \text{ s} = 28.24 \text{ s} \approx 28 \text{ s}$ .

- (e) For this part of the problem, the rocket has  $v_0 = 0 \text{ m/s}$ ,  $a = -9.80 \text{ m/s}^2$ , and a displacement of  $-962 \text{ m}$  (it falls from a height of  $962 \text{ m}$  to the ground). Find the velocity upon reaching the Earth from Eq. 2-12c.

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow$$

$$v = \pm \sqrt{v_0^2 + 2a(y - y_0)} = \pm \sqrt{0 + 2(-9.80 \text{ m/s}^2)(-962 \text{ m})} = -137.3 \text{ m/s} \approx \boxed{-137 \text{ m/s}}$$

The negative root was chosen because the rocket is moving downward, which is the negative direction.

- (f) The time for the rocket to fall back to the Earth is found from Eq. 2-12a.

$$v = v_0 + at \rightarrow t_{\text{fall}} = \frac{v - v_0}{a} = \frac{-137.3 \text{ m/s} - 0}{-9.80 \text{ m/s}^2} = 14.01 \text{ s}$$

Thus the total time for the entire flight is  $t = 28.24 \text{ s} + 14.01 \text{ s} = 42.25 \text{ s} \approx \boxed{42 \text{ s}}$ .

65. Choose upward to be the positive direction, and  $y_0 = 0$  to be the location of the nozzle. The initial velocity is  $v_0$ , the acceleration is  $a = -9.80 \text{ m/s}^2$ , the final location is  $y = -1.8 \text{ m}$ , and the time of flight is  $t = 2.5 \text{ s}$ . Using Eq. 2-12b and substituting  $y$  for  $x$  gives the following.

$$y = y_0 + v_0 t + \frac{1}{2} a t^2 \rightarrow$$

$$v_0 = \frac{y - \frac{1}{2} a t^2}{t} = \frac{-1.8 \text{ m} - \frac{1}{2}(-9.80 \text{ m/s}^2)(2.5 \text{ s})^2}{2.5 \text{ s}} = 11.53 \text{ m/s} \approx \boxed{12 \text{ m/s}}$$

66. Choose downward to be the positive direction, and take  $y_0 = 0$  to be the height where the package was released. The initial velocity is  $v_0 = -6.40 \text{ m/s}$ , the acceleration is  $a = 9.80 \text{ m/s}^2$ , and the displacement of the package will be  $y = 105 \text{ m}$ . The time to reach the ground can be found from Eq. 2-12b, with  $x$  replaced by  $y$ .

$$y = y_0 + v_0 t + \frac{1}{2} a t^2 \rightarrow t^2 + \frac{2v_0}{a} t - \frac{2y}{a} = 0 \rightarrow t^2 + \frac{2(-6.40 \text{ m/s})}{9.80 \text{ m/s}^2} t - \frac{2(105 \text{ m})}{9.80 \text{ m/s}^2} = 0 \rightarrow$$

$$t^2 - 1.306t - 21.43 = 0 \rightarrow t = \frac{1.306 \pm \sqrt{(1.306)^2 - 4(-21.43)}}{2} = 5.33 \text{ s}, -4.02 \text{ s}$$

The correct time is the positive answer,  $\boxed{t = 5.33 \text{ s}}$ .

67. (a) Choose  $y = 0$  to be the ground level, and positive to be upward. Then  $y = 0 \text{ m}$ ,  $y_0 = 15 \text{ m}$ ,  $a = -g$ , and  $t = 0.83 \text{ s}$  describe the motion of the balloon. Use Eq. 2-12b.

$$y = y_0 + v_0 t + \frac{1}{2} a t^2 \rightarrow$$

$$v_0 = \frac{y - y_0 - \frac{1}{2} a t^2}{t} = \frac{0 - 15 \text{ m} - \frac{1}{2}(-9.80 \text{ m/s}^2)(0.83 \text{ s})^2}{(0.83 \text{ s})} = -14.01 \text{ m/s} \approx \boxed{-14 \text{ m/s}}$$

So the speed is  $\boxed{14 \text{ m/s}}$ .

- (b) Consider the change in velocity from being released to being at Roger's room, using Eq. 2-12c.

$$v^2 = v_0^2 + 2a\Delta y \rightarrow \Delta y = \frac{v^2 - v_0^2}{2a} = \frac{-(-14.01 \text{ m/s})^2}{2(-9.80 \text{ m/s}^2)} = 10.01 \text{ m}$$

Thus the balloons are coming from 25 m above the ground.

68. Choose upward to be the positive direction, and  $y_0 = 0$  to be the level from which the ball was thrown. The initial velocity is  $v_0$ , the instantaneous velocity is  $v = 13 \text{ m/s}$ , the acceleration is  $a = -9.80 \text{ m/s}^2$ , and the location of the window is  $y = 18 \text{ m}$ .

- (a) Using Eq. 2-12c and substituting  $y$  for  $x$ , we have

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow$$

$$v_0 = \pm \sqrt{v^2 - 2a(y - y_0)} = \pm \sqrt{(13 \text{ m/s})^2 - 2(-9.80 \text{ m/s}^2)(18 \text{ m})} = 22.84 \text{ m/s} \approx \boxed{23 \text{ m/s}}$$

Choose the positive value because the initial direction is upward.

- (b) At the top of its path, the velocity will be 0, and so we can use the initial velocity as found above, along with Eq. 2-12c.

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow y = y_0 + \frac{v^2 - v_0^2}{2a} = 0 + \frac{0 - (22.84 \text{ m/s})^2}{2(-9.80 \text{ m/s}^2)} = 26.62 \text{ m} \approx \boxed{27 \text{ m}}$$

- (c) We want the time elapsed from throwing (velocity  $v_0 = 22.84 \text{ m/s}$ ) to reaching the window (velocity  $v = 13 \text{ m/s}$ ). Use Eq. 2-12a.

$$v = v_0 + at \rightarrow t = \frac{v - v_0}{a} = \frac{13 \text{ m/s} - 22.84 \text{ m/s}}{-9.80 \text{ m/s}^2} = 1.004 \text{ s} \approx \boxed{1.0 \text{ s}}$$

- (d) We want the time elapsed from the window ( $v_0 = 13 \text{ m/s}$ ) to reaching the street ( $v = -22.84 \text{ m/s}$ ). Use Eq. 2-12a.

$$v = v_0 + at \rightarrow t = \frac{v - v_0}{a} = \frac{-22.84 \text{ m/s} - 13 \text{ m/s}}{-9.80 \text{ m/s}^2} = 3.657 \text{ s} \approx \boxed{3.7 \text{ s}}$$

The total time from throwing to reaching the street again is  $1.004 \text{ s} + 3.657 \text{ s} = 4.661 \text{ s} \approx 4.7 \text{ s}$ .

69. Choose downward to be the positive direction, and  $y_0 = 0$  to be the height from which the stone is dropped. Call the location of the top of the window  $y_{\text{top}}$ . From the distance and time given you can use Eq. 2-12b to find the velocity at the top of the window,  $v_{\text{top}}$ . That speed can then be used to find the height from which the stone was dropped.

$$(y_{\text{bottom}} - y_{\text{top}}) = v_{\text{top}}t + \frac{1}{2}at^2 \rightarrow$$

$$v_{\text{top}} = \frac{(y_{\text{bottom}} - y_{\text{top}}) - \frac{1}{2}at^2}{t} = \frac{2.2 \text{ m} - \frac{1}{2}(9.80 \text{ m/s}^2)(0.28 \text{ s})^2}{(0.28 \text{ s})} = 6.485 \text{ m/s}$$

$$v_{\text{top}}^2 = v_0^2 + 2a(y_{\text{top}} - y_0) \rightarrow y_{\text{top}} = \frac{v_{\text{top}}^2 - v_0^2}{2a} - y_0 = \frac{(6.485 \text{ m/s})^2}{2(9.80 \text{ m/s}^2)} = 2.146 \text{ m} \approx \boxed{2.1 \text{ m}}$$

70. Choose up to be the positive direction, so  $a = -g$ . Let the ground be the  $y = 0$  location. As an intermediate result, the velocity at the bottom of the window can be found from the data given. Assume the rocket is at the bottom of the window at  $t = 0$ , and use Eq. 2-12b.

$$y_{\text{top of window}} = y_{\text{bottom of window}} + v_{\text{bottom of window}} t_{\text{pass window}} + \frac{1}{2} a t_{\text{pass window}}^2 \rightarrow$$

$$10.0 \text{ m} = 8.0 \text{ m} + v_{\text{bottom of window}} (0.15 \text{ s}) + \frac{1}{2} (-9.80 \text{ m/s}^2) (0.15 \text{ s})^2 \rightarrow v_{\text{bottom of window}} = 14.07 \text{ m/s}$$

Now use the velocity at the bottom of the window with Eq. 2-12c to find the launch velocity, assuming the launch velocity was achieved at the ground level.

$$v_{\text{bottom of window}}^2 = v_{\text{launch}}^2 + 2a(y - y_0) \rightarrow$$

$$v_{\text{launch}} = \sqrt{v_{\text{bottom of window}}^2 - 2a(y - y_0)} = \sqrt{(14.07 \text{ m/s})^2 - 2(-9.80 \text{ m/s}^2)(8.0 \text{ m})} = 18.84 \text{ m/s}$$

$$\approx \boxed{18.8 \text{ m/s}}$$

The maximum height can also be found from Eq. 2-12c, using the launch velocity and a velocity of 0 at the maximum height.

$$v_{\text{maximum height}}^2 = v_{\text{launch}}^2 + 2a(y_{\text{max}} - y_0) \rightarrow$$

$$y_{\text{max}} = y_0 + \frac{v_{\text{maximum height}}^2 - v_{\text{launch}}^2}{2a} = \frac{-(18.84 \text{ m/s})^2}{2(-9.80 \text{ m/s}^2)} = \boxed{18.1 \text{ m}}$$

71. Choose up to be the positive direction. Let the bottom of the cliff be the  $y = 0$  location. The equation of motion for the dropped ball is  $y_{\text{ball}} = y_0 + v_0 t + \frac{1}{2} a t^2 = 55.0 \text{ m} + \frac{1}{2} (-9.80 \text{ m/s}^2) t^2$ . The equation of motion for the thrown stone is  $y_{\text{stone}} = y_0 + v_0 t + \frac{1}{2} a t^2 = (24.0 \text{ m/s}) t + \frac{1}{2} (-9.80 \text{ m/s}^2) t^2$ . Set the two equations equal and solve for the time of the collision. Then use that time to find the location of either object.

$$y_{\text{ball}} = y_{\text{stone}} \rightarrow 55.0 \text{ m} + \frac{1}{2} (-9.80 \text{ m/s}^2) t^2 = (24.0 \text{ m/s}) t + \frac{1}{2} (-9.80 \text{ m/s}^2) t^2 \rightarrow$$

$$55.0 \text{ m} = (24.0 \text{ m/s}) t \rightarrow t = \frac{55.0 \text{ m}}{24.0 \text{ m/s}} = 2.292 \text{ s}$$

$$y_{\text{ball}} = y_0 + v_0 t + \frac{1}{2} a t^2 = 55.0 \text{ m} + 0 + \frac{1}{2} (-9.80 \text{ m/s}^2) (2.292 \text{ s})^2 = \boxed{29.3 \text{ m}}$$

$$y_{\text{stone}} = y_0 + v_0 t + \frac{1}{2} a t^2 = 0 + (24.0 \text{ m/s}) (2.292 \text{ s}) + \frac{1}{2} (-9.80 \text{ m/s}^2) (2.292 \text{ s})^2 = \boxed{29.3 \text{ m}}$$

72. The displacement is found from the integral of the velocity, over the given time interval.

$$\Delta x = \int_{t_1}^{t_2} v dt = \int_{t=1.3\text{s}}^{t=3.6\text{s}} (25 + 18t) dt = \left( 25t + 9t^2 \right) \Big|_{t=1.3\text{s}}^{t=3.6\text{s}} = \left[ 25(3.6) + 9(3.6)^2 \right] - \left[ 25(1.3) + 9(1.3)^2 \right]$$

$$= 158.93 \text{ m} \approx \boxed{1.6 \times 10^2 \text{ m}}$$

73. (a) The velocity is the integral of the acceleration.

$$a = \frac{dv}{dt} \rightarrow dv = a dt \rightarrow dv = A\sqrt{t} dt \rightarrow \int_{v_0}^v dv = A \int_0^t \sqrt{t} dt \rightarrow$$

$$v - v_0 = \frac{2}{3} A t^{3/2} \rightarrow v = v_0 + \frac{2}{3} A t^{3/2} \rightarrow \boxed{v = 7.5 \text{ m/s} + \frac{2}{3} (3.0 \text{ m/s}^{5/2}) t^{3/2}}$$

- (b) The displacement is the integral of the velocity.

$$v = \frac{dx}{dt} \rightarrow dx = v dt \rightarrow dx = \left( v_0 + \frac{2}{3} A t^{3/2} \right) dt \rightarrow$$

$$\int_{0 \text{ m}}^x dx = \int_0^t \left( v_0 + \frac{2}{3} A t^{3/2} \right) dt \rightarrow x = v_0 t + \frac{2}{3} \cdot \frac{2}{5} A t^{5/2} = \boxed{(7.5 \text{ m/s}) t + \frac{4}{15} (3.0 \text{ m/s}^{5/2}) t^{5/2}}$$

(c)  $a(t = 5.0 \text{ s}) = (3.0 \text{ m/s}^{5/2}) \sqrt{5.0 \text{ s}} = \boxed{6.7 \text{ m/s}^2}$

$$v(t = 5.0 \text{ s}) = 7.5 \text{ m/s} + \frac{2}{3} (3.0 \text{ m/s}^{5/2}) (5.0 \text{ s})^{3/2} = 29.86 \text{ m/s} \approx \boxed{3.0 \times 10^1 \text{ m/s}}$$

$$x(t = 5.0 \text{ s}) = (7.5 \text{ m/s})(5.0 \text{ s}) + \frac{4}{15} (3.0 \text{ m/s}^{5/2}) (5.0 \text{ s})^{5/2} = 82.22 \text{ m} \approx \boxed{82 \text{ m}}$$

74. (a) The velocity is found by integrating the acceleration with respect to time. Note that with the substitution given in the hint, the initial value of  $u$  is  $u_0 = g - kv_0 = g$ .

$$a = \frac{dv}{dt} \rightarrow dv = a dt \rightarrow dv = (g - kv) dt \rightarrow \frac{dv}{g - kv} = dt$$

Now make the substitution that  $u \equiv g - kv$ .

$$u \equiv g - kv \rightarrow dv = -\frac{du}{k} \quad \frac{dv}{g - kv} = dt \rightarrow -\frac{du}{k} \frac{1}{u} = dt \rightarrow \frac{du}{u} = -k dt$$

$$\int_g^u \frac{du}{u} = -k \int_0^t dt \rightarrow \ln u \Big|_g^u = -kt \rightarrow \ln \frac{u}{g} = -kt \rightarrow u = g e^{-kt} = g - kv \rightarrow$$

$$\boxed{v = \frac{g}{k} (1 - e^{-kt})}$$

- (b) As  $t$  goes to infinity, the value of the velocity is  $v_{\text{term}} = \lim_{t \rightarrow \infty} \frac{g}{k} (1 - e^{-kt}) = \boxed{\frac{g}{k}}$ . We also note that

if the acceleration is zero (which happens at terminal velocity), then  $a = g - kv = 0 \rightarrow$

$$v_{\text{term}} = \frac{g}{k}.$$

75. Choose the upward direction to be positive, and  $y_0 = 0$  to be the level from which the object is thrown. The initial velocity is  $v_0$  and the velocity at the top of the path is  $v = 0 \text{ m/s}$ . The height at the top of the path can be found from Eq. 2-12c with  $x$  replaced by  $y$ .

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow y - y_0 = \frac{-v_0^2}{2a}.$$

From this we see that the displacement is inversely proportional to the acceleration, and so if the acceleration is reduced by a factor of 6 by going to the Moon, and the initial velocity is unchanged, then the displacement increases by a factor of 6.

76. (a) For the free-falling part of the motion, choose downward to be the positive direction, and  $y_0 = 0$  to be the height from which the person jumped. The initial velocity is  $v_0 = 0$ , the acceleration is  $a = 9.80 \text{ m/s}^2$ , and the location of the net is  $y = 18.0 \text{ m}$ . Find the speed upon reaching the net from Eq. 2-12c with  $x$  replaced by  $y$ .

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow$$

$$v = \pm \sqrt{0 + 2a(y - 0)} = \pm \sqrt{2(9.80 \text{ m/s}^2)(18.0 \text{ m})} = 18.78 \text{ m/s}$$

The positive root is selected since the person is moving downward.

For the net-stretching part of the motion, choose downward to be the positive direction, and  $y_0 = 18.0 \text{ m}$  to be the height at which the person first contacts the net. The initial velocity is  $v_0 = 18.78 \text{ m/s}$ , the final velocity is  $v = 0$ , and the location at the stretched position is  $y = 19.0 \text{ m}$ . Find the acceleration from Eq. 2-12c with  $x$  replaced by  $y$ .

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow$$

$$a = \frac{v^2 - v_0^2}{2(y - y_0)} = \frac{0^2 - (18.78 \text{ m/s})^2}{2(1.0 \text{ m})} = -176 \text{ m/s}^2 \approx \boxed{-180 \text{ m/s}^2}$$

This is about  $18 g$ 's.

- (b) For the acceleration to be smaller, in the above equation we see that the displacement would have to be larger. This means that the net should be "loosened."

77. We treat the value of  $30 g$ 's as if it had 2 significant figures. The initial velocity of the car is

$$v_0 = (95 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) = 26.39 \text{ m/s.}$$

Choose  $x_0 = 0$  to be location at which the deceleration begins. We have  $v = 0 \text{ m/s}$  and  $a = -30g = -294 \text{ m/s}^2$ . Find the displacement from Eq. 2-12c.

$$v^2 = v_0^2 + 2a(x - x_0) \rightarrow x = x_0 + \frac{v^2 - v_0^2}{2a} = 0 + \frac{0 - (26.39 \text{ m/s})^2}{2(-294 \text{ m/s}^2)} = 1.18 \text{ m} \approx \boxed{1.2 \text{ m}}$$

78. We are given that  $x(t) = 2.0 - 3.6t + 1.7t^2$ , where  $x$  is in meters and  $t$  is in seconds.

- (a) The value of 2.0 must have units of meters, and is the initial position of the ball. The value of 3.6 must have units of m/s, and is the initial speed of the ball – the speed at  $t = 0$ . Note that the ball is initially moving in the negative direction, since  $-3.6$  is used. The value of 1.7 must have units of  $\text{m/s}^2$ , and based on Eq. 2-12b is  $\frac{1}{2}$  the acceleration of the ball.
- (b) As given above, the units of 2.0 are meters, the units of 3.6 are m/s, and the units of 1.7 are  $\text{m/s}^2$ .

$$(c) \quad x(1.0 \text{ s}) = 2.0 \text{ m} - (3.6 \text{ m/s})(1.0 \text{ s}) + (1.7 \text{ m/s}^2)(1.0 \text{ s})^2 = \boxed{0.1 \text{ m}}$$

$$x(2.0 \text{ s}) = 2.0 \text{ m} - (3.6 \text{ m/s})(2.0 \text{ s}) + (1.7 \text{ m/s}^2)(2.0 \text{ s})^2 = \boxed{1.6 \text{ m}}$$

$$x(3.0 \text{ s}) = 2.0 \text{ m} - (3.6 \text{ m/s})(3.0 \text{ s}) + (1.7 \text{ m/s}^2)(3.0 \text{ s})^2 = \boxed{6.5 \text{ m}}$$

$$(d) \quad \bar{v} = \frac{\Delta x}{\Delta t} = \frac{6.5 \text{ m} - 0.1 \text{ m}}{2.0 \text{ s}} = \boxed{3.2 \text{ m/s}}$$

79. (a) The sounds will not occur at equal time intervals because the longer any particular bolt falls, the higher its speed. The bolts all start from rest and all have the same acceleration, so at any moment in time, they will all have the same speed. However, they have different distances to travel in reaching the floor and therefore will be falling for different lengths of time. The farther a bolt falls, and thus the later a bolt hits the tin plate, the longer it has been accelerating and therefore the faster it is moving.
- (b) With equal distances between bolts, each successive bolt, having fallen a longer time when its predecessor reaches the plate, will have a higher average velocity and thus travel the inter-bolt distance in shorter periods of time. Thus the sounds will occur with smaller and smaller intervals between sounds. Thus the time between “clinks” will decrease as the string falls.
- (c) To hear the sounds at equal intervals, the bolts would have to be tied at distances corresponding to equal time intervals. The first bolt (call it bolt # 0) is touching the plate. Since each bolt has an initial speed of 0, the distance of fall and time of fall for each bolt are related to each other by  $d_i = \frac{1}{2} g t_i^2$ . For bolt # 1,  $d_1 = \frac{1}{2} g t_1^2$ . For bolt # 2, we want  $t_2 = 2t_1$ , so  $d_2 = \frac{1}{2} g t_2^2 = \frac{1}{2} g (2t_1)^2 = 4(\frac{1}{2} g t_1^2) = 4d_1$ . Likewise  $t_3 = 3t_1$ , which leads to  $d_3 = 9d_1$ ;  $t_4 = 4t_1$ , which leads to  $d_4 = 16d_1$ , and so on. If the distance from the bolt initially on the pan to the next bolt is  $d_1$ , then the distance from that bolt to the next one is  $3d_1$ , the distance to the next bolt is  $5d_1$ , and so on. The accompanying table shows these relationships in a simpler format.

| Bolt # | Height above floor | Time to fall  | Distance between bolts |
|--------|--------------------|---------------|------------------------|
| 0      | 0                  | 0             |                        |
| 1      | $d_1$              | $t_1$         | $d_1$                  |
| 2      | $d_2 = 4 d_1$      | $t_2 = 2 t_1$ | $3 d_1$                |
| 3      | $d_3 = 9 d_1$      | $t_3 = 3 t_1$ | $5 d_1$                |
| 4      | $d_4 = 16 d_1$     | $t_4 = 4 t_1$ | $7 d_1$                |
| 5      | $d_5 = 25 d_1$     | $t_5 = 5 t_1$ | $9 d_1$                |

80. Choose downward to be the positive direction, and the origin to be at the top of the building. The barometer has  $y_0 = 0$ ,  $v_0 = 0$ , and  $a = g = 9.8 \text{ m/s}^2$ . Use Eq. 2-12b to find the height of the building, with  $x$  replaced by  $y$ .

$$y = y_0 + v_0 t + \frac{1}{2} a t^2 = 0 + 0 + \frac{1}{2} (9.8 \text{ m/s}^2) t^2$$

$$y_{t=2.0} = \frac{1}{2} (9.8 \text{ m/s}^2) (2.0 \text{ s})^2 = 20 \text{ m} \quad y_{t=2.3} = \frac{1}{2} (9.8 \text{ m/s}^2) (2.3 \text{ s})^2 = 26 \text{ m}$$

The difference in the estimates is 6 m. If we assume the height of the building is the average of the two measurements, then the % difference in the two values is  $\frac{6 \text{ m}}{23 \text{ m}} \times 100 = \boxed{26\%}$ .

81. The speed limit is  $40 \text{ km/h} \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) = 11.11 \text{ m/s}$ .

- (a) For your motion, you would need to travel  $(10 + 15 + 50 + 15 + 70) \text{ m} = 160 \text{ m}$  to get the front of the car to the third stoplight. The time to travel the 160 m is found using the distance and the speed limit.

$$\Delta x = \bar{v} \Delta t \rightarrow \Delta t = \frac{\Delta x}{\bar{v}} = \frac{160 \text{ m}}{11.11 \text{ m/s}} = 14.40 \text{ s}$$

**No**, you cannot make it to the third light without stopping, since it takes you longer than 13.0 seconds to reach the third light.

- (b) The second car needs to travel 165 m before the third light turns red. This car accelerates from  $v_0 = 0 \text{ m/s}$  to a maximum of  $v = 11.11 \text{ m/s}$  with  $a = 2.00 \text{ m/s}^2$ . Use Eq. 2-12a to determine the duration of that acceleration.

$$v = v_0 + at \rightarrow t_{\text{acc}} = \frac{v - v_0}{a} = \frac{11.11 \text{ m/s} - 0 \text{ m/s}}{2.00 \text{ m/s}^2} = 5.556 \text{ s}$$

The distance traveled during that time is found from Eq. 2-12b.

$$(x - x_0)_{\text{acc}} = v_0 t_{\text{acc}} + \frac{1}{2} a t_{\text{acc}}^2 = 0 + \frac{1}{2} (2.00 \text{ m/s}^2) (5.556 \text{ s})^2 = 30.87 \text{ m}$$

Since 5.556 s have elapsed, there are  $13.0 - 5.556 = 7.444 \text{ s}$  remaining to clear the intersection.

The car travels another 7.444 s at a speed of 11.11 m/s, covering a distance of  $\Delta x_{\text{constant speed}} = v_{\text{avg}} t =$

$$(11.11 \text{ m/s})(7.444 \text{ s}) = 82.70 \text{ m. Thus the total distance is } 30.87 \text{ m} + 82.70 \text{ m} = 113.57 \text{ m.}$$

**No**, the car cannot make it through all three lights without stopping.

The car has to travel another 51.43 m to clear the third intersection, and is traveling at a speed of 11.11 m/s. Thus the front of the car would clear the intersection a time

$$t = \frac{\Delta x}{v} = \frac{51.43 \text{ m}}{11.11 \text{ m/s}} = \boxed{4.6 \text{ s}} \text{ after the light turns red.}$$

82. (a) Choose downward to be the positive direction, and  $y_0 = 0$  to be the level from which the car was dropped. The initial velocity is  $v_0 = 0$ , the final location is  $y = H$ , and the acceleration is  $a = g$ . Find the final velocity from Eq. 2-12c, replacing  $x$  with  $y$ .

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow v = \pm \sqrt{v_0^2 + 2a(y - y_0)} = \pm \sqrt{2gH}.$$

The speed is the magnitude of the velocity,  $v = \sqrt{2gH}$ .

- (b) Solving the above equation for the height, we have that  $H = \frac{v^2}{2g}$ . Thus for a collision of

$v = 35 \text{ km/h}$ , the corresponding height is as follows.

$$H = \frac{v^2}{2g} = \frac{\left[ (35 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) \right]^2}{2(9.80 \text{ m/s}^2)} = 4.823 \text{ m} \approx \boxed{4.8 \text{ m}}$$

- (c) For a collision of  $v = 95 \text{ km/h}$ , the corresponding height is the following.

$$H = \frac{v^2}{2g} = \frac{\left[ (95 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) \right]^2}{2(9.80 \text{ m/s}^2)} = 35.53 \text{ m} \approx \boxed{36 \text{ m}}$$

83. Choose downward to be the positive direction, and  $y_0 = 0$  to be at the roof from which the stones are dropped. The first stone has an initial velocity of  $v_0 = 0$  and an acceleration of  $a = g$ . Eqs. 2-12a and 2-12b (with  $x$  replaced by  $y$ ) give the velocity and location, respectively, of the first stone as a function of time.

$$v = v_0 + at \rightarrow v_1 = gt_1 \quad y = y_0 + v_0 t + \frac{1}{2} at^2 \rightarrow y_1 = \frac{1}{2} gt_1^2$$

The second stone has the same initial conditions, but its elapsed time is  $t_2 = t_1 - 1.50\text{ s}$ , and so has velocity and location equations as follows.

$$v_2 = g(t_1 - 1.50\text{ s}) \quad y_2 = \frac{1}{2}g(t_1 - 1.50\text{ s})^2$$

The second stone reaches a speed of  $v_2 = 12.0\text{ m/s}$  at a time given by the following.

$$t_2 = \frac{v_2}{g} = t_1 - 1.50\text{ s} \rightarrow t_1 = 1.50\text{ s} + \frac{v_2}{g} = 1.50\text{ s} + \frac{12.0\text{ m/s}}{9.80\text{ m/s}^2} = 2.724\text{ s}$$

The location of the first stone at that time is  $y_1 = \frac{1}{2}gt_1^2 = \frac{1}{2}(9.80\text{ m/s}^2)(2.724\text{ s})^2 = 36.36\text{ m}$ .

The location of the second stone at that time is

$$y_2 = \frac{1}{2}g(t_1 - 1.50\text{ s})^2 = \frac{1}{2}(9.80\text{ m/s}^2)(2.724 - 1.50\text{ s})^2 = 7.34\text{ m}.$$

Thus the distance between the two stones is  $y_1 - y_2 = 36.36\text{ m} - 7.34\text{ m} = \boxed{29.0\text{ m}}$ .

84. For the motion in the air, choose downward to be the positive direction, and  $y_0 = 0$  to be at the height of the diving board. Then diver has  $v_0 = 0$ , (assuming the diver does not jump upward or downward),  $a = g = 9.80\text{ m/s}^2$ , and  $y = 4.0\text{ m}$  when reaching the surface of the water. Find the diver's speed at the water's surface from Eq. 2-12c, with  $x$  replaced by  $y$ .

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow v = \pm\sqrt{v_0^2 + 2a(y - y_0)} = \sqrt{0 + 2(9.80\text{ m/s}^2)(4.0\text{ m})} = 8.85\text{ m/s}$$

For the motion in the water, again choose down to be positive, but redefine  $y_0 = 0$  to be at the surface of the water. For this motion,  $v_0 = 8.85\text{ m/s}$ ,  $v = 0$ , and  $y - y_0 = 1.8\text{ m}$ . Find the acceleration from Eq. 2-12c, with  $x$  replaced by  $y$ .

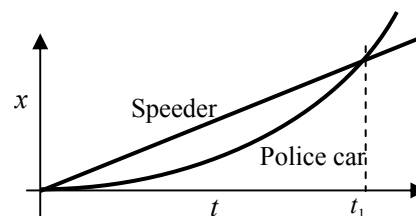
$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow a = \frac{v^2 - v_0^2}{2(y - y_0)} = \frac{0 - (8.85\text{ m/s})^2}{2(1.8\text{ m})} = \boxed{-22\text{ m/s}^2}$$

The negative sign indicates that the acceleration is directed upwards.

85. Take the origin to be the location where the speeder passes the police car. The speeder's constant speed is  $v_{\text{speeder}} = (140\text{ km/h})\left(\frac{1\text{ m/s}}{3.6\text{ km/h}}\right) = 38.89\text{ m/s}$ , and the location of the speeder as a function of time is given by  $x_{\text{speeder}} = v_{\text{speeder}}t_{\text{speeder}} = (38.89\text{ m/s})t_{\text{speeder}}$ . The police car has an initial velocity of  $v_0 = 0\text{ m/s}$  and a constant acceleration of  $a_{\text{police}}$ . The location of the police car as a function of time is given by Eq. 2-12b.

$$x_{\text{police}} = v_0t + \frac{1}{2}at^2 = \frac{1}{2}a_{\text{police}}t_{\text{police}}^2$$

- (a) The position vs. time graphs would qualitatively look like the graph shown here.



- (b) The time to overtake the speeder occurs when the speeder has gone a distance of 850 m. The time is found using the speeder's equation from above.

$$850\text{ m} = (38.89\text{ m/s})t_{\text{speeder}} \rightarrow t_{\text{speeder}} = \frac{850\text{ m}}{38.89\text{ m/s}} = 21.86\text{ s} \approx \boxed{22\text{ s}}$$

- (c) The police car's acceleration can be calculated knowing that the police car also had gone a distance of 850 m in a time of 21.86 s.

$$850 \text{ m} = \frac{1}{2} a_p (21.86 \text{ s})^2 \rightarrow a_p = \frac{2(850 \text{ m})}{(21.86 \text{ s})^2} = 3.558 \text{ m/s}^2 \approx \boxed{3.6 \text{ m/s}^2}$$

- (d) The speed of the police car at the overtaking point can be found from Eq. 2-12a.

$$v = v_0 + at = 0 + (3.558 \text{ m/s}^2)(21.86 \text{ s}) = 77.78 \text{ m/s} \approx \boxed{78 \text{ m/s}}$$

Note that this is exactly twice the speed of the speeder, and so is 280 km/h.

- (e) The police officer would not want to pass the car at that high speed, because then he would go past the car for a long distance before being able to pull the speeder over. The police officer would not have a constant acceleration, but instead, once he gets close to the speeder, will start to slow down so as to match the speeder's velocity and pull in close behind the speeder.

86. Choose downward to be the positive direction, and  $y_0 = 0$  to be at the height of the bridge. Agent Bond has an initial velocity of  $v_0 = 0$ , an acceleration of  $a = g$ , and will have a displacement of  $y = 15 \text{ m} - 3.5 \text{ m} = 11.5 \text{ m}$ . Find the time of fall from Eq. 2-12b with  $x$  replaced by  $y$ .

$$y = y_0 + v_0 t + \frac{1}{2} a t^2 \rightarrow t = \sqrt{\frac{2y}{a}} = \sqrt{\frac{2(11.5 \text{ m})}{9.80 \text{ m/s}^2}} = 1.532 \text{ s}$$

If the truck is approaching with  $v = 25 \text{ m/s}$ , then he needs to jump when the truck is a distance away given by  $d = vt = (25 \text{ m/s})(1.532 \text{ s}) = 38.3 \text{ m}$ . Convert this distance into "poles."

$$d = (38.3 \text{ m})(1 \text{ pole}/25 \text{ m}) = 1.53 \text{ poles}$$

So he should jump when the truck is about 1.5 poles away from the bridge.

87. Assume that  $y_0 = 0$  for each child is the level at which the child loses contact with the trampoline surface. Choose upward to be the positive direction.

- (a) The second child has  $v_{02} = 4.0 \text{ m/s}$ ,  $a = -g = -9.80 \text{ m/s}^2$ , and  $v = 0 \text{ m/s}$  at the maximum height position. Find the child's maximum height from Eq. 2-12c, with  $x$  replaced by  $y$ .

$$v^2 = v_{02}^2 + 2a(y_2 - y_0) \rightarrow y_2 = y_0 + \frac{v^2 - v_{02}^2}{2a} = 0 + \frac{0 - (4.0 \text{ m/s})^2}{2(-9.80 \text{ m/s}^2)} = 0.8163 \text{ m} \approx \boxed{0.82 \text{ m}}$$

- (b) Since the first child can bounce up to one-and-a-half times higher than the second child, the first child can bounce up to a height of  $1.5(0.8163 \text{ m}) = 1.224 \text{ m} = y_1 - y_0$ . Eq. 2-12c is again used to find the initial speed of the first child.

$$v^2 = v_{01}^2 + 2a(y_1 - y_0) \rightarrow v_{01} = \pm \sqrt{v^2 - 2a(y_1 - y_0)} = \sqrt{0 - 2(-9.80 \text{ m/s}^2)(1.224 \text{ m})} = 4.898 \text{ m/s} \approx \boxed{4.9 \text{ m/s}}$$

The positive root was chosen since the child was initially moving upward.

- (c) To find the time that the first child was in the air, use Eq. 2-12b with a total displacement of 0, since the child returns to the original position.

$$y = y_0 + v_{01}t_1 + \frac{1}{2}at_1^2 \rightarrow 0 = (4.898 \text{ m/s})t_1 + \frac{1}{2}(-9.80 \text{ m/s}^2)t_1^2 \rightarrow t_1 = 0 \text{ s}, 0.9996 \text{ s}$$

The time of 0 s corresponds to the time the child started the jump, so the correct answer is 1.0 s.

88. First consider the “uphill lie,” in which the ball is being putted down the hill. Choose  $x_0 = 0$  to be the ball’s original location, and the direction of the ball’s travel as the positive direction. The final velocity of the ball is  $v = 0$  m/s, the acceleration of the ball is  $a = -1.8$  m/s<sup>2</sup>, and the displacement of the ball will be  $x - x_0 = 6.0$  m for the first case and  $x - x_0 = 8.0$  m for the second case. Find the initial velocity of the ball from Eq. 2-12c.

$$v^2 = v_0^2 + 2a(x - x_0) \rightarrow v_0 = \sqrt{v^2 - 2a(x - x_0)} = \begin{cases} \sqrt{0 - 2(-1.8 \text{ m/s}^2)(6.0 \text{ m})} = 4.648 \text{ m/s} \\ \sqrt{0 - 2(-1.8 \text{ m/s}^2)(8.0 \text{ m})} = 5.367 \text{ m/s} \end{cases}$$

The range of acceptable velocities for the uphill lie is  $\boxed{4.6 \text{ m/s to } 5.4 \text{ m/s}}$ , a spread of 0.719 m/s if more digits are kept.

Now consider the “downhill lie,” in which the ball is being putted up the hill. Use a very similar set-up for the problem, with the basic difference being that the acceleration of the ball is now  $a = -2.6$  m/s<sup>2</sup>. Find the initial velocity of the ball from Eq. 2-12c.

$$v^2 = v_0^2 + 2a(x - x_0) \rightarrow v_0 = \sqrt{v^2 - 2a(x - x_0)} = \begin{cases} \sqrt{0 - 2(-2.6 \text{ m/s}^2)(6.0 \text{ m})} = 5.586 \text{ m/s} \\ \sqrt{0 - 2(-2.6 \text{ m/s}^2)(8.0 \text{ m})} = 6.450 \text{ m/s} \end{cases}$$

The range of acceptable velocities for the downhill lie is  $\boxed{5.6 \text{ m/s to } 6.5 \text{ m/s}}$ , a spread of 0.864 m/s if more digits are kept. Because the range of acceptable velocities is smaller for putting down the hill, more control in putting is necessary, and so putting the ball downhill (the “uphill lie”) is more difficult.

89. The car’s initial speed is  $v_0 = (35 \text{ km/h})\left(\frac{1 \text{ m/s}}{3.6 \text{ km/h}}\right) = 9.722 \text{ m/s}$ .

Case I: trying to stop. The constraint is, with the braking deceleration of the car ( $a = -5.8$  m/s<sup>2</sup>), can the car stop in a 28 m displacement? The 2.0 seconds has no relation to this part of the problem. Using Eq. 2-12c, the distance traveled during braking is as follows.

$$(x - x_0) = \frac{v^2 - v_0^2}{2a} = \frac{0 - (9.722 \text{ m/s})^2}{2(-5.8 \text{ m/s}^2)} = 8.14 \text{ m} \quad \boxed{\text{She can stop the car in time.}}$$

Case II: crossing the intersection. The constraint is, with the acceleration of the car

$$\left[ a = \left( \frac{65 \text{ km/h} - 45 \text{ km/h}}{6.0 \text{ s}} \right) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) = 0.9259 \text{ m/s}^2 \right], \text{ can she get through the intersection}$$

(travel 43 meters) in the 2.0 seconds before the light turns red? Using Eq. 2-12b, the distance traveled during the 2.0 sec is

$$(x - x_0) = v_0 t + \frac{1}{2} a t^2 = (9.722 \text{ m/s})(2.0 \text{ s}) + \frac{1}{2} (0.9259 \text{ m/s}^2)(2.0 \text{ s})^2 = 21.3 \text{ m}.$$

$\boxed{\text{She should stop.}}$

90. The critical condition is that the total distance covered by the passing car and the approaching car must be less than 500 m so that they do not collide. The passing car has a total displacement composed of several individual parts. These are: i) the 10 m of clear room at the rear of the truck; ii) the 20 m length of the truck; iii) the 10 m of clear room at the front of the truck; and iv) the distance the truck travels. Since the truck travels at a speed of  $\bar{v} = 18 \text{ m/s}$ , the truck will have a displacement of  $\Delta x_{\text{truck}} = (18 \text{ m/s})t$ . Thus the total displacement of the car during passing is
- $$\Delta x_{\text{passing car}} = 40 \text{ m} + (18 \text{ m/s})t.$$

To express the motion of the car, we choose the origin to be at the location of the passing car when the decision to pass is made. For the passing car, we have an initial velocity of  $v_0 = 18 \text{ m/s}$  and an acceleration of  $a = 0.60 \text{ m/s}^2$ . Find  $\Delta x_{\text{passing car}}$  from Eq. 2-12b.

$$\Delta x_{\text{passing car}} = x_c - x_0 = v_0 t + \frac{1}{2} a t^2 = (18 \text{ m/s})t + \frac{1}{2} (0.60 \text{ m/s}^2) t^2$$

Set the two expressions for  $\Delta x_{\text{passing car}}$  equal to each other in order to find the time required to pass.

$$40 \text{ m} + (18 \text{ m/s})t_{\text{pass}} = (18 \text{ m/s})t_{\text{pass}} + \frac{1}{2} (0.60 \text{ m/s}^2) t_{\text{pass}}^2 \rightarrow 40 \text{ m} = \frac{1}{2} (0.60 \text{ m/s}^2) t_{\text{pass}}^2 \rightarrow$$

$$t_{\text{pass}} = \sqrt{\frac{80}{0.60}} \text{ s} = 11.55 \text{ s}$$

Calculate the displacements of the two cars during this time.

$$\Delta x_{\text{passing car}} = 40 \text{ m} + (18 \text{ m/s})(11.55 \text{ s}) = 247.9 \text{ m}$$

$$\Delta x_{\text{approaching car}} = v_{\text{approaching}} t = (25 \text{ m/s})(11.55 \text{ s}) = 288.75 \text{ m}$$

Thus the two cars together have covered a total distance of  $247.9 \text{ m} + 288.75 \text{ m} = 536.65 \text{ m}$ , which is more than allowed. The car should not pass.

91. For the falling rock, choose downward to be the positive direction, and  $y_0 = 0$  to be the height from which the stone is dropped. The initial velocity is  $v_0 = 0 \text{ m/s}$ , the acceleration is  $a = g$ , the final position is  $y = H$ , and the time of fall is  $t_1$ . Using Eq. 2-12b with  $y$  substituting for  $x$ , we have
- $$H = y_0 + v_0 t + \frac{1}{2} g t^2 = 0 + 0 + \frac{1}{2} g t_1^2. \text{ For the sound wave, use the constant speed equation that}$$

$$v_{\text{snd}} = \frac{\Delta x}{\Delta t} = \frac{H}{T - t_1}, \text{ which can be rearranged to give } t_1 = T - \frac{H}{v_{\text{snd}}}, \text{ where } T = 4.1 \text{ s is the total time}$$

elapsed from dropping the rock to hearing the sound. Insert this expression for  $t_1$  into the equation for  $H$  from the stone, and solve for  $H$ .

$$H = \frac{1}{2} g \left( T - \frac{H}{v_{\text{snd}}} \right)^2 \rightarrow \frac{g}{2 v_{\text{snd}}^2} H^2 - \left( \frac{gT}{v_{\text{snd}}} + 1 \right) H + \frac{1}{2} g T^2 = 0 \rightarrow$$

$$4.2388 \times 10^{-5} H^2 - 1.1182 H + 82.369 = 0 \rightarrow H = 73.9 \text{ m}, 2.63 \times 10^4 \text{ m}$$

If the larger answer is used in  $t_1 = T - \frac{H}{v_s}$ , a negative time of fall results, and so the physically correct answer is the smaller one:  $H = 74 \text{ m}$ .

92. The speed of the conveyor belt is found from Eq. 2-2 for average velocity.

$$\Delta x = \bar{v} \Delta t \rightarrow \bar{v} = \frac{\Delta x}{\Delta t} = \frac{1.2 \text{ m}}{2.8 \text{ min}} = 0.4286 \text{ m/min} \approx \boxed{0.43 \text{ m/min}}$$

The rate of burger production, assuming the spacing given is center to center, can be found as follows.

$$\left( \frac{1 \text{ burger}}{0.25 \text{ m}} \right) \left( \frac{0.4286 \text{ m}}{1 \text{ min}} \right) = \boxed{1.7 \frac{\text{burgers}}{\text{min}}}$$

93. (a) Choose up to be the positive direction. Let the throwing height of both objects be the  $y = 0$  location, and so  $y_0 = 0$  for both objects. The acceleration of both objects is  $a = -g$ . The equation of motion for the rock, using Eq. 2-12b, is  $y_{\text{rock}} = y_0 + v_{0 \text{ rock}} t + \frac{1}{2} a t^2 = v_{0 \text{ rock}} t - \frac{1}{2} g t^2$ , where  $t$  is the time elapsed from the throwing of the rock. The equation of motion for the ball, being thrown 1.00 s later, is  $y_{\text{ball}} = y_0 + v_{0 \text{ ball}} (t - 1.00 \text{ s}) + \frac{1}{2} a (t - 1.00 \text{ s})^2 = v_{0 \text{ ball}} (t - 1.00 \text{ s}) - \frac{1}{2} g (t - 1.00 \text{ s})^2$ . Set the two equations equal (meaning the two objects are at the same place) and solve for the time of the collision.

$$\begin{aligned} y_{\text{rock}} = y_{\text{ball}} &\rightarrow v_{0 \text{ rock}} t - \frac{1}{2} g t^2 = v_{0 \text{ ball}} (t - 1.00 \text{ s}) - \frac{1}{2} g (t - 1.00 \text{ s})^2 \rightarrow \\ (15.0 \text{ m/s}) t - \frac{1}{2} (9.80 \text{ m/s}^2) t^2 &= (22.0 \text{ m/s}) (t - 1.00 \text{ s}) - \frac{1}{2} (9.80 \text{ m/s}^2) (t - 1.00 \text{ s})^2 \rightarrow \\ (-16.8) t &= -26.9 \\ (16.8 \text{ m/s}) t &= (26.9 \text{ m}) \rightarrow t = \boxed{1.60 \text{ s}} \text{ after the rock was thrown} \end{aligned}$$

- (b) Use the time for the collision to find the position of either object.

$$\begin{aligned} y_{\text{rock}} &= v_{0 \text{ rock}} t - \frac{1}{2} g t^2 = (15.0 \text{ m/s}) (1.60 \text{ s}) - \frac{1}{2} (9.80 \text{ m/s}^2) (1.60 \text{ s})^2 = 11.46 \text{ m} \approx \boxed{11.5 \text{ m}} \\ y_{\text{ball}} &= v_{0 \text{ ball}} (t - 1.00 \text{ s}) - \frac{1}{2} g (t - 1.00 \text{ s})^2 = (22.0 \text{ m/s}) (0.60 \text{ s}) - \frac{1}{2} (9.80 \text{ m/s}^2) (0.60 \text{ s})^2 \\ &= 11.44 \text{ m} \end{aligned}$$

- (c) Now the ball is thrown first, and so  $y_{\text{ball}} = v_{0 \text{ ball}} t - \frac{1}{2} g t^2$  and

$$y_{\text{rock}} = v_{0 \text{ rock}} (t - 1.00 \text{ s}) - \frac{1}{2} g (t - 1.00 \text{ s})^2. \text{ Again set the two equations equal to find the time of collision.}$$

$$\begin{aligned} y_{\text{ball}} = y_{\text{rock}} &\rightarrow v_{0 \text{ ball}} t - \frac{1}{2} g t^2 = v_{0 \text{ rock}} (t - 1.00 \text{ s}) - \frac{1}{2} g (t - 1.00 \text{ s})^2 \rightarrow \\ (22.0 \text{ m/s}) t - \frac{1}{2} (9.80 \text{ m/s}^2) t^2 &= (15.0 \text{ m/s}) (t - 1.00 \text{ s}) - \frac{1}{2} (9.80 \text{ m/s}^2) (t - 1.00 \text{ s})^2 \rightarrow \\ (22.0 \text{ m/s}) t &= (15.0 \text{ m/s}) t - 15 + 9.8 t - 4.9 \\ (2.80 \text{ m/s}) t &= 19.9 \text{ m} \rightarrow t = 7.11 \text{ s after the ball was thrown} \end{aligned}$$

But this answer can be deceptive. Where do the objects collide?

$$y_{\text{ball}} = v_{0 \text{ ball}} t - \frac{1}{2} g t^2 = (22.0 \text{ m/s})(7.11 \text{ s}) - \frac{1}{2} (9.80 \text{ m/s}^2)(7.11 \text{ s})^2 = -91.3 \text{ m}$$

$$y_{\text{rock}} = v_{0 \text{ rock}} (t - 1.00 \text{ s}) - \frac{1}{2} g (t - 1.00 \text{ s})^2 = (15.0 \text{ m/s})(6.11 \text{ s}) - \frac{1}{2} (9.80 \text{ m/s}^2)(6.11 \text{ s})^2 = -91.3 \text{ m}$$

Thus, assuming they were thrown from ground level, they collide below ground level, which cannot happen. Thus they never collide. Or, they had to be more than 91.3 m above the ground at their launch point.

94. (a) During the interval from A to B, it is moving in the negative direction, because its displacement is negative.
- (b) During the interval from A to B, it is speeding up, because the magnitude of its slope is increasing (changing from less steep to more steep).
- (c) During the interval from A to B, the acceleration is negative, because the graph is concave downward, indicating that the slope is getting more negative, and thus the acceleration is negative.
- (d) During the interval from D to E, it is moving in the positive direction, because the displacement is positive.
- (e) During the interval from D to E, it is speeding up, because the magnitude of its slope is increasing (changing from less steep to more steep).
- (f) During the interval from D to E, the acceleration is positive, because the graph is concave upward, indicating the slope is getting more positive, and thus the acceleration is positive.
- (g) During the interval from C to D, the object is not moving in either direction.
- The velocity and acceleration are both 0.

95. This problem can be analyzed as a series of three one-dimensional motions; the acceleration phase, the constant speed phase, and the deceleration phase. The maximum speed of the train is:

$$(95 \text{ km/h}) \left( \frac{1 \text{ m/s}}{3.6 \text{ km/h}} \right) = 26.39 \text{ m/s}$$

In the acceleration phase, the initial velocity is  $v_0 = 0 \text{ m/s}$ , the acceleration is  $a = 1.1 \text{ m/s}^2$ , and the final velocity is  $v = 26.39 \text{ m/s}$ . Find the elapsed time for the acceleration phase from Eq. 2-12a.

$$v = v_0 + at \rightarrow t_{\text{acc}} = \frac{v - v_0}{a} = \frac{26.39 \text{ m/s} - 0}{1.1 \text{ m/s}^2} = 23.99 \text{ s}$$

Find the displacement during the acceleration phase from Eq. 2-12b.

$$(x - x_0)_{\text{acc}} = v_0 t + \frac{1}{2} a t^2 = 0 + \frac{1}{2} (1.1 \text{ m/s}^2) (23.99 \text{ s})^2 = 316.5 \text{ m}$$

In the deceleration phase, the initial velocity is  $v_0 = 26.39 \text{ m/s}$ , the acceleration is  $a = -2.0 \text{ m/s}^2$ , and the final velocity is  $v = 0 \text{ m/s}$ . Find the elapsed time for the deceleration phase from Eq. 2-12a.

$$v = v_0 + at \rightarrow t_{\text{dec}} = \frac{v - v_0}{a} = \frac{0 - 26.39 \text{ m/s}}{-2.0 \text{ m/s}^2} = 13.20 \text{ s}$$

Find the distance traveled during the deceleration phase from Eq. 2-12b.

$$(x - x_0)_{\text{dec}} = v_0 t + \frac{1}{2} a t^2 = (26.39 \text{ m/s})(13.20 \text{ s}) + \frac{1}{2} (-2.0 \text{ m/s}^2)(13.20 \text{ s})^2 = 174.1 \text{ m}$$

The total elapsed time and distance traveled for the acceleration / deceleration phases are:

$$t_{\text{acc}} + t_{\text{dec}} = 23.99 \text{ s} + 13.20 \text{ s} = 37.19 \text{ s}$$

$$(x - x_0)_{\text{acc}} + (x - x_0)_{\text{dec}} = 316.5 \text{ m} + 174.1 \text{ m} = 491 \text{ m}$$

- (a) If the stations are spaced  $3.0 \text{ km} = 3000 \text{ m}$  apart, then there is a total of  $\frac{15000 \text{ m}}{3000 \text{ m}} = 5$  inter-

station segments. A train making the entire trip would thus have a total of 5 inter-station segments and 4 stops of 22 s each at the intermediate stations. Since 491 m is traveled during acceleration and deceleration,  $3000 \text{ m} - 491 \text{ m} = 2509 \text{ m}$  of each segment is traveled at an average speed of  $\bar{v} = 26.39 \text{ m/s}$ . The time for that 2509 m is given by  $\Delta x = \bar{v} \Delta t \rightarrow$

$$\Delta t_{\text{constant speed}} = \frac{\Delta x}{\bar{v}} = \frac{2509 \text{ m}}{26.39 \text{ m/s}} = 95.07 \text{ s. Thus a total inter-station segment will take } 37.19 \text{ s} +$$

$95.07 \text{ s} = 132.26 \text{ s}$ . With 5 inter-station segments of 132.26 s each, and 4 stops of 22 s each, the total time is given by  $t_{3.0 \text{ km}} = 5(132.26 \text{ s}) + 4(22 \text{ s}) = 749 \text{ s} = \boxed{12.5 \text{ min}}$ .

- (b) If the stations are spaced  $5.0 \text{ km} = 5000 \text{ m}$  apart, then there is a total of  $\frac{15000 \text{ m}}{5000 \text{ m}} = 3$  inter-

station segments. A train making the entire trip would thus have a total of 3 inter-station segments and 2 stops of 22 s each at the intermediate stations. Since 491 m is traveled during acceleration and deceleration,  $5000 \text{ m} - 491 \text{ m} = 4509 \text{ m}$  of each segment is traveled at an average speed of  $\bar{v} = 26.39 \text{ m/s}$ . The time for that 4509 m is given by  $d = \bar{v} t \rightarrow$

$$t = \frac{d}{\bar{v}} = \frac{4509 \text{ m}}{26.39 \text{ m/s}} = 170.86 \text{ s. Thus a total inter-station segment will take } 37.19 \text{ s} + 170.86 \text{ s} =$$

$208.05 \text{ s}$ . With 3 inter-station segments of 208.05 s each, and 2 stops of 22 s each, the total time is given by  $t_{5.0 \text{ km}} = 3(208.05 \text{ s}) + 2(22 \text{ s}) = 668 \text{ s} = \boxed{11.1 \text{ min}}$ .

96. To find the average speed for the entire race, we must take the total distance divided by the total time. If one lap is a distance of  $L$ , then the total distance will be  $10L$ . The time elapsed at a given

constant speed is given by  $t = d/v$ , so the time for the first 9 laps would be  $t_1 = \frac{9L}{196.0 \text{ km/h}}$ , and

the time for the last lap would be  $t_2 = L/v_2$ , where  $v_2$  is the average speed for the last lap. Write an expression for the average speed for the entire race, and then solve for  $v_2$ .

$$\bar{v} = \frac{d_{\text{total}}}{t_1 + t_2} = \frac{10L}{\frac{9L}{196.0 \text{ km/h}} + \frac{L}{v_2}} = 200.0 \text{ km/h} \rightarrow$$

$$v_2 = \frac{1}{\frac{10}{200.0 \text{ km/h}} - \frac{9}{196.0 \text{ km/h}}} = \boxed{245.0 \text{ km/h}}$$

97. Since all of the motion and most of the acceleration is downward, we will call downward the positive direction. Let the parachutist's initial position be  $y_0 = 0$  m, and their initial speed is  $v_0 = 0$  m/s. We break the motion up into two constant-acceleration segments. The final position, duration, velocity, and acceleration for the first segment are represented by  $y_1$ ,  $t_1$ ,  $v_1$ , and  $a_1$ , respectively. Note that the final velocity for the first segment is the initial velocity for the second segment.

First segment:  $y_1 = y_0 + v_0 t_1 + \frac{1}{2} a_1 t_1^2 \rightarrow t_1 = \sqrt{\frac{2y_1}{a_1}} = \sqrt{\frac{2(75 \text{ m})}{9.8 \text{ m/s}^2}} = 3.912 \text{ s}$

$$v_1 = a_1 t_1 = (9.8 \text{ m/s}^2)(3.912 \text{ s}) = 38.34 \text{ m/s}$$

$$v_2^2 = v_1^2 + 2a_2 \Delta y_2 \rightarrow \Delta y_2 = \frac{v_2^2 - v_1^2}{2a_2} = \frac{(1.5 \text{ m/s})^2 - (38.34 \text{ m/s})^2}{2(-1.5 \text{ m/s}^2)} = 489.2 \text{ m}$$

Second segment:

$$v_2 = v_1 + a_2 t_2 \rightarrow t_2 = \frac{v_2 - v_1}{a_2} = \frac{1.5 \text{ m/s} - 38.34 \text{ m/s}}{-1.5 \text{ m/s}^2} = 24.56 \text{ s}$$

(a) Total height:  $75 \text{ m} + 489.2 \text{ m} = 564.2 \text{ m} \approx \boxed{560 \text{ m}}$

(b) Total time:  $3.912 \text{ s} + 24.56 \text{ s} = 28.472 \text{ s} \approx \boxed{28 \text{ s}}$

98. As shown in Example 2-18, the speed with which the ball was thrown upward is the same as its speed on returning to the ground. From the symmetry of the two motions (both motions have speed = 0 at top, have same distance traveled, and have same acceleration), the time for the ball to rise is the same as the time for the ball to fall, 1.4 s. Choose upward to be the positive direction, and the origin to be at the level where the ball was thrown. For the ball,  $v = 0$  at the top of the motion, and  $a = -g$ . Find the initial velocity from Eq. 2-12a.

$$v = v_0 + at \rightarrow v_0 = v - at = 0 - (-9.80 \text{ m/s}^2)(1.4 \text{ s}) = 13.72 \text{ m/s} \approx \boxed{14 \text{ m/s}}$$

99. To find the distance, we divide the motion of the robot into three segments. First, the initial acceleration from rest; second, motion at constant speed; and third, deceleration back to rest.

$$d_1 = v_0 t + \frac{1}{2} a_1 t_1^2 = 0 + \frac{1}{2} (0.20 \text{ m/s}^2)(4.5 \text{ s})^2 = 2.025 \text{ m}$$

$$v_1 = a_1 t_1 = (0.20 \text{ m/s}^2)(4.5 \text{ s}) = 0.90 \text{ m/s}$$

$$d_2 = v_1 t_2 = (0.90 \text{ m/s})(68 \text{ s}) = 61.2 \text{ m} \quad v_2 = v_1 = 0.90 \text{ m/s}$$

$$d_3 = v_2 t_3 + \frac{1}{2} a_1 t_1^2 = (0.90 \text{ m/s})(2.5 \text{ s}) + \frac{1}{2} (-0.40 \text{ m/s}^2)(2.5 \text{ s})^2 = 1.0 \text{ m}$$

$$d = d_1 + d_2 + d_3 = 2.025 \text{ m} + 61.2 \text{ m} + 1.0 \text{ m} = 64.225 \text{ m} \approx \boxed{64 \text{ m}}$$

100. Choose upward to be the positive direction, and the origin to be at the level where the ball was thrown. The velocity at the top is  $v = 0$ , and the ball will have an acceleration of  $a = -g$ . If the maximum height that the ball reaches is  $y = H$ , then the relationship between the initial velocity and the maximum height can be found from Eq. 2-12c, with  $x$  replaced by  $y$ .

$$v^2 = v_0^2 + 2a(y - y_0) \rightarrow 0 = v_0^2 + 2(-g)H \rightarrow H = v_0^2 / 2g$$

It is given that  $v_{0 \text{ Bill}} = 1.5 v_{0 \text{ Joe}}$ , so  $\frac{H_{\text{Bill}}}{H_{\text{Joe}}} = \frac{(v_{0 \text{ Bill}})^2 / 2g}{(v_{0 \text{ Joe}})^2 / 2g} = \frac{(v_{0 \text{ Bill}})^2}{(v_{0 \text{ Joe}})^2} = 1.5^2 = 2.25 \approx \boxed{2.3}$ .

101. (a) Multiply the reading rate times the bit density to find the bit reading rate.

$$N = \frac{1.2 \text{ m}}{1 \text{ s}} \times \frac{1 \text{ bit}}{0.28 \times 10^{-6} \text{ m}} = \boxed{4.3 \times 10^6 \text{ bits/s}}$$

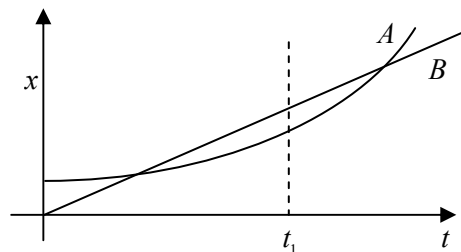
- (b) The number of excess bits is  $N - N_0$ .

$$N - N_0 = 4.3 \times 10^6 \text{ bits/s} - 1.4 \times 10^6 \text{ bits/s} = 2.9 \times 10^6 \text{ bits/s}$$

$$\frac{N - N_0}{N} = \frac{2.9 \times 10^6 \text{ bits/s}}{4.3 \times 10^6 \text{ bits/s}} = 0.67 = \boxed{67\%}$$

102. (a) The two bicycles will have the same velocity at any time when the instantaneous slopes of their  $x$  vs.  $t$  graphs are the same. That occurs near the time  $t_1$  as marked on the graph.

- (b) Bicycle A has the larger acceleration, because its graph is concave upward, indicating a positive acceleration. Bicycle B has no acceleration because its graph has a constant slope.



- (c) The bicycles are passing each other at the times when the two graphs cross, because they both have the same position at that time. The graph with the steepest slope is the faster bicycle, and so is the one that is passing at that instant. So at the first crossing, bicycle B is passing bicycle A. At the second crossing, bicycle A is passing bicycle B.
- (d) Bicycle B has the highest instantaneous velocity at all times until the time  $t_1$ , where both graphs have the same slope. For all times after  $t_1$ , bicycle A has the highest instantaneous velocity. The largest instantaneous velocity is for bicycle A at the latest time shown on the graph.
- (e) The bicycles appear to have the same average velocity. If the starting point of the graph for a particular bicycle is connected to the ending point with a straight line, the slope of that line is the average velocity. Both appear to have the same slope for that “average” line.

103. In this problem, note that  $a < 0$  and  $x > 0$ . Take your starting position as 0. Then your position is given by Eq. 2-12b,  $x_1 = v_M t + \frac{1}{2} a t^2$ , and the other car's position is given by  $x_2 = x + v_A t$ . Set the two positions equal to each other and solve for the time of collision. If this time is negative or imaginary, then there will be no collision.

$$x_1 = x_2 \rightarrow v_M t + \frac{1}{2} a t^2 = x + v_A t \rightarrow \frac{1}{2} a t^2 + (v_M - v_A) t - x = 0$$

$$t = \frac{(v_A - v_M) \pm \sqrt{(v_M - v_A)^2 - 4 \frac{1}{2} a (-x)}}{2 \frac{1}{2} a}$$

$$\text{No collision: } (v_M - v_A)^2 - 4 \frac{1}{2} a (-x) < 0 \rightarrow \boxed{x > \frac{(v_M - v_A)^2}{-2a}}$$